6 (a) It is given that

$$f(x) = x^3 - x^2 + x - 6$$

Use the factor theorem to show that $(x - 2)$ is a factor of $f(x)$.

[2 marks]

6 (b) Find the quadratic factor of $f(x)$.

[1 mark]

6 (c) Hence, show that there is only one real solution to $f(x) = 0$

[3 marks]

6 (d) Find the exact value of x that solves

$$e^{3x} - e^{2x} + e^x - 6 = 0$$

[3 marks]