

Q	Marking instructions	AO	Marks	Typical solution
13(a)(i)	Rearranges to make x the subject by isolating x terms or Swaps x and y and isolates y terms	1.1a	M1	$y = \frac{2x + 3}{x - 2}$ $xy - 2y = 2x + 3$ $xy - 2x = 2y + 3$ $x(y - 2) = 2y + 3$ $x = \frac{2y + 3}{y - 2}$ $f^{-1}(x) = \frac{2x + 3}{x - 2} \quad x \neq 2$
	Obtains correct rearrangement and factorises ACF PI by final correct answer	1.1b	A1	
	Obtains $f^{-1}(x)$ and states domain Must use fully correct notation	2.5	R1	
	Subtotal		3	
13(a)(ii)	Obtains any valid expression in x for $ff(x)$ Can be left unsimplified ISW	1.1b	B1	$ff(x) = x$
	Subtotal		1	
13(b)(i)	Deduces the greatest value of g by evaluating $g(4)$	2.2a	B1	$g(4) = 6$ Vertex at (1.25, -1.5625) $\{y : -1.5625 \leq y \leq 6\}$
	Obtains the minimum value of g	3.1a	B1	
	States the range using their finite greatest value and finite minimum value using set notation or interval notation Accept $[-1.5625, 6]$ in interval notation For set notation - use of none curly brackets or commas scores R0	2.5	R1F	
	Subtotal		3	
13(b)(ii)	Demonstrates that g is a many to one function by using an appropriate method eg Sketches the function Or Evaluates $g(x)$ at two points that give the same answer.	2.4	E1	$g(0) = 0 = g(2.5)$ g is many to one so it does not have an inverse.
	Deduces that g is many to one and states that g has no inverse Or Explains that g is not one to one and states that g has no inverse	2.2a	E1	
	Subtotal		2	

13(c)	Substitutes $f(x)$ into $g(x)$ correctly	1.1a	M1	$gf(x) = \frac{2\left(\frac{2x+3}{x-2}\right)^2 - 5\left(\frac{2x+3}{x-2}\right)}{2}$ $= \frac{2(2x+3)^2 - 5(2x+3)(x-2)}{2(x-2)^2}$ $= \frac{2(4x^2+12x+9) - 5(2x^2-x-6)}{2(x^2-4x+4)}$ $= \frac{48 + 29x - 2x^2}{2x^2 - 8x + 8}$
	Obtains common denominator of $2(x-2)^2$ or $(x-2)^2$ correctly The fraction(s) must have the fully correct structure	1.1b	A1	
	Expands at least two quadratics correctly	1.1a	M1	
	Completes rigorous argument to show the required result Must have expanded all three quadratics correctly Terms in the numerator and denominator can be in any order AG	2.1	R1	
Subtotal			4	
13(d)	States $g(x) = 2$ or States $2x^2 - 5x - 4 = 0$ PI by solving correct quadratic PI by sight of $\frac{5+\sqrt{57}}{4}$ or $\frac{5-\sqrt{57}}{4}$	3.1a	M1	$2x^2 - 5x - 4 = 0$ $x = \frac{5 \pm \sqrt{57}}{4}$ $a > 0 \text{ since } 0 \leq x \leq 4$ $a = \frac{5 + \sqrt{57}}{4}$
	Determines the exact value of a giving a clear reason for the rejection of the negative root	2.4	R1	
Subtotal			2	
Question Total			15	