

Q	Marking instructions	AO	Marks	Typical solution
8	<p>Begins integration by parts by writing</p> $u = x \quad v' = \sin 4x$ $u' = 1 \quad v = A \cos 4x$ <p>PI by</p> $Ax \cos 4x - A \int (\cos 4x) dx$ <p>Or</p> $u = \sin 4x \quad v' = x$ $u' = A \cos 4x \quad v = Bx^2$ <p>PI by</p> $Px^2 \sin 4x - Q \int (x^2 \cos 4x) dx$	3.1a	M1	$u = x \quad v' = \sin 4x$ $u' = 1 \quad v = -\frac{1}{4} \cos 4x$ $\left[-\frac{1}{4} x \cos 4x \right]_0^{\frac{\pi}{2}} + \frac{1}{4} \int_0^{\frac{\pi}{2}} (\cos 4x) dx$ $= \left[-\frac{1}{4} x \cos 4x + \frac{1}{16} \sin 4x \right]_0^{\frac{\pi}{2}}$ $= \left(-\frac{\pi}{8} \cos \frac{4\pi}{2} + \frac{1}{16} \sin \frac{4\pi}{2} \right) - \left(0 \times \cos 0 + \frac{1}{16} \sin 0 \right)$ $= -\frac{\pi}{8}$
	<p>Selects the correct method for integration by parts</p> $u = x \quad v' = \sin 4x$ $u' = 1 \quad v = A \cos 4x$ <p>PI by $Ax \cos 4x - A \int (\cos 4x) dx$</p>	1.1a	M1	
	<p>Substitutes their u, u', v, v' of either of the above forms into the integration by parts formula.</p> <p>Eg</p> $Px \cos 4x - P \int (\cos 4x) dx$ $Px^2 \sin 4x - Q \int (x^2 \cos 4x) dx$ $\frac{x^2}{2} \sin 4x - \int (2x^2 \cos 4x) dx$ <p>PI by $-\frac{1}{4} x \cos 4x + \frac{1}{16} \sin 4x$</p>	1.1a	M1	
	<p>Obtains</p> $-\frac{1}{4} x \cos 4x - \frac{1}{4} \int (-\cos 4x) dx$ <p>Condone missing dx</p> <p>PI by $-\frac{1}{4} x \cos 4x + \frac{1}{16} \sin 4x$</p>	1.1b	A1	
	<p>Completes integration by parts to obtain $-\frac{1}{4} x \cos 4x + B \sin 4x$ with $B \neq \pm 1$</p>	1.1a	M1	
	<p>Completes reasoned argument by explicitly substituting correct limits into</p> $-\frac{1}{4} x \cos 4x + \frac{1}{16} \sin 4x$	2.1	R1	

To obtain $-\frac{\pi}{8}$

Accept

$$\left(-\frac{\pi}{8} \cos 2\pi + \frac{1}{16} \sin 2\pi \right) = 0$$

AG

Question 8 Total

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