

Q	Marking instructions	AO	Mark	Typical solution
7(a)	Sketches any cubic graph, crossing the x -axis in three places	1.2	B1	
	Sketches any cubic graph with a positive coefficient of x^3	1.2	B1	
7(b)(i)	Differentiates to obtain $f'(x)$ Two terms with at least one correct - either $3x^2$ or $6px$	1.1a	M1	For a turning point $f'(x) = 0$ $f(x) = x^3 + 3px^2 + q$ $f'(x) = 3x^2 + 6px$
	Solves $3x^2 + 6px = 0$ to obtain $x = 0$ or $x = -2p$ or Substitutes $x = 0$ in $f'(x) = 3x^2 + 6px$ and obtains 0	1.1b	A1	$3x^2 + 6px = 0$ $3x(x + 2p) = 0$ $x = 0$ $x = -2p$
	Obtains the correct two roots $x = 0$ and $x = -2p$ OE and states why there must be a turning point referring to root $x = 0$	2.4	R1	Since one of the roots is $x = 0$ there must be a turning point on the y axis
7(b)(ii)	Deduces that turning point at $x = -2p$ is a maximum or deduces that turning point $x = 0$ is a minimum May have been seen in part (b)(i) Accept a sketch showing correct relative positions of turning points	2.2a	B1	Since $p > 0$ $x = -2p$ is the maximum $x = 0$ is the minimum $f(0) = q$ $f(-2p) = (-2p)^3 + 3p(-2p)^2 + q$ $= 4p^3 + q$
	Substitutes their $x = -2p$ into $f(x)$	1.1a	M1	$-4p^3 < q < 0$
	Obtains correct $f(0) = q$ and $f(-2p) = 4p^3 + q$	1.1b	A1	
	Deduces either $q < 0$ or $-4p^3 < q$ Condone \leq	2.2a	R1	
	Deduces $-4p^3 < q < 0$ CAO	2.2a	R1	
Total			10	