

Q	Marking instructions	AO	Mark	Typical solution
7(a)(i)	Identifies the error lies in step 1 without contradiction.	2.3	E1	Mistake is $\frac{1}{a} + \frac{1}{b} = \frac{2}{a+b}$
	Subtotal		1	
7(a)(ii)	Recalls correct addition Accept $\frac{b}{ab} + \frac{a}{ab}$	1.1b	M1	$\frac{1}{a} + \frac{1}{b} = \frac{a+b}{ab}$ $a + b$ is rational and ab is rational and therefore
	Completes rigorous argument to complete proof. Must state that ab is rational (and non-zero) and $a + b$ is rational and conclude that $\frac{1}{a} + \frac{1}{b}$ or $\frac{a+b}{ab}$ is rational	2.1	R1	$\frac{1}{a} + \frac{1}{b}$ is rational.
	Subtotal		2	
7(b)	States assumption to begin proof by contradiction may PI by $\frac{a}{b} - x = \frac{c}{d}$ or $x - \frac{a}{b} = \frac{c}{d}$	3.1a	M1	Assume that the difference between a rational and an irrational number is rational. $\frac{a}{b} - x = \frac{c}{d}$
	Uses language and notation correctly to state initial assumptions: States their a, b, c and d are integers and x is irrational do not accept the irrational written as a fraction Condone missing $b, d \neq 0$	2.5	A1	Where a, b, c and d are integers, $b, d \neq 0$ and x is irrational
	Demonstrates that x can be expressed as a rational number by obtaining $x = \frac{ad - cb}{bd}$ OE	1.1b	M1	$x = \frac{a}{b} - \frac{c}{d}$ $= \frac{ad}{bd} - \frac{cb}{bd}$ $= \frac{ad - cb}{bd}$
	Completes rigorous argument to prove the required result, clearly explaining where the contradiction lies with ALL assumptions correct at the start (including $b, d \neq 0$)	2.1	R1	Hence x is rational. This is a contradiction hence the difference of any rational number and any irrational number is irrational.
	Subtotal		4	
	Question Total		7	