

Q	Marking instructions	AO	Marks	Typical solution
9(a)	Identifies and clearly defines variable for radius of cylinder. Can be shown on diagram or can be implied by use in $V = \pi r^2 h$	2.5	B1	Radius of cylinder = $r$ $h^2 + r^2 = R^2$ $V = \pi r^2 h$
	Uses Pythagoras to connect $h$ , $r$ and $R$	3.1a	M1	
	Eliminates the radius variable to form an expression for the volume of the cylinder in terms of $h$ , completing argument to show given result. Condone undefined $r$	2.1	R1	$V = \pi(R^2 - h^2)h$ $= \pi R^2 h - \pi h^3$
<b>Subtotal</b>			<b>3</b>	
9(b)	Differentiates the expression for volume w.r.t. $h$ with at least one term correct.	3.1a	M1	$\frac{dV}{dh} = \pi R^2 - 3\pi h^2$
	Obtains correct $\frac{dV}{dh}$	1.1b	A1	For maximum volume $\frac{dV}{dh} = 0$
	Explains that their derivative w.r.t $h$ equals zero for a maximum or stationary point	2.4	E1	$\Rightarrow R^2 - 3h^2 = 0$
	Equates volume derivative w.r.t. $h$ to zero and correctly obtains a value for $h$ in terms of $R$	1.1a	M1	$h^2 = \frac{R^2}{3} \Rightarrow h = \frac{R}{\sqrt{3}}$
	Substitutes their $h$ , in terms of $R$ , from derivative w.r.t. $h$ into volume formula.	1.1a	M1	Hence volume
	Obtains the correct max volume in the form $kR^3 - pR^3$ or better	3.2a	A1	$V = \pi R^2 \frac{R}{\sqrt{3}} - \pi \left( \frac{R}{\sqrt{3}} \right)^3$ $= \frac{2\sqrt{3}\pi R^3}{9}$
	Justifies correct volume in the form $kR^3 - pR^3$ or better form is the maximum eg: <ul style="list-style-type: none"><li>• <math>V = 0</math> when <math>h=0</math> or <math>R</math> and <math>V&gt;0</math> in between.</li><li>• Sketches shape of graph passing through the origin with (min on negative side) and max on positive side</li><li>• Obtains <math>\frac{d^2V}{dh^2} = -6\pi h &lt; 0</math></li></ul> NB R1 can be awarded even if E1 is not awarded.	2.1	R1	$\frac{d^2V}{dh^2} = -6\pi h$ When $h = \frac{R}{\sqrt{3}}$ $\frac{d^2V}{dh^2} < 0$ Therefore maximum

	<b>Subtotal</b>		<b>7</b>	
	<b>Question Total</b>		<b>10</b>	