

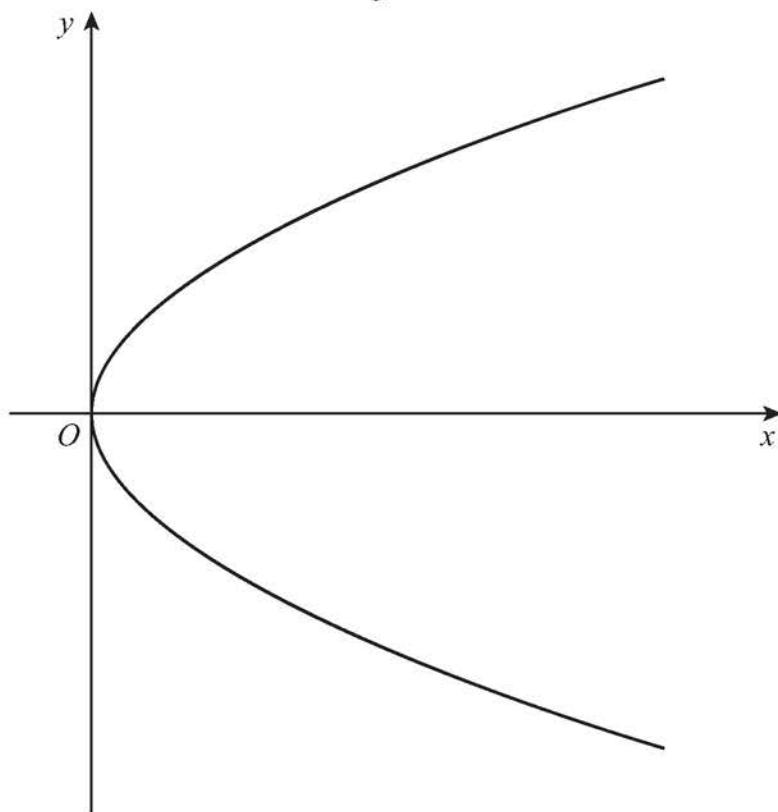
8

The curve defined by the parametric equations

$$x = t^2 \quad \text{and} \quad y = 2t \quad -\sqrt{2} \leq t \leq \sqrt{2}$$

is shown in **Figure 1** below.

Figure 1



- 8 (a)** Find a Cartesian equation of the curve in the form $y^2 = f(x)$

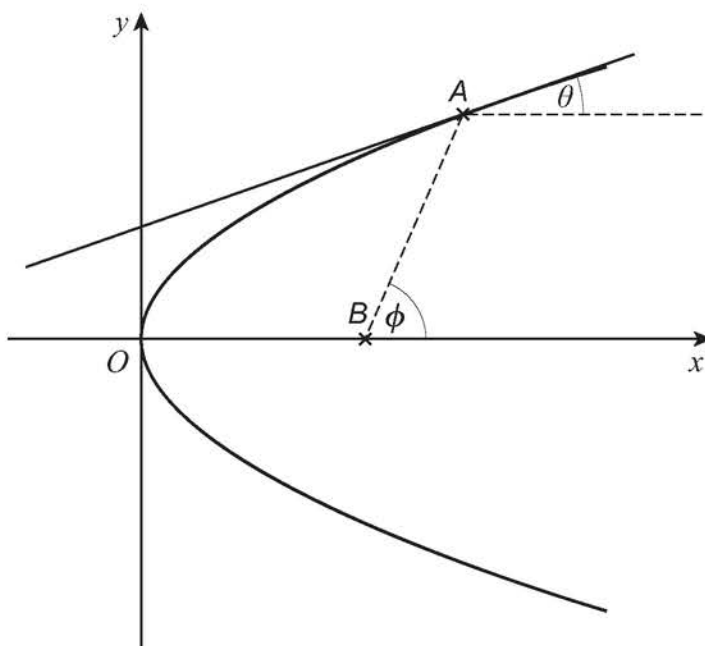
[2 marks]

- 8 (b)** The point A lies on the curve where $t = a$

The tangent to the curve at A is at an angle θ to a line through A parallel to the x -axis.

The point B has coordinates $(1, 0)$

The line AB is at an angle ϕ to the x -axis.



- 8 (b) (i)** By considering the gradient of the curve, show that

$$\tan \theta = \frac{1}{a}$$

[3 marks]

- 8 (b) (ii)** Find $\tan \phi$ in terms of a .

[2 marks]

- 8 (b) (iii)** Show that $\tan 2\theta = \tan \phi$

[3 marks]