

| Q | Marking instructions | AO | Marks | Typical solution |
|-----------------|--|------|----------|-----------------------------|
| 10(a) | Obtains a domain excluding negatives or excluding 3 Condone $x > 0$ | 1.1a | M1 | $\{x: x \geq 0, x \neq 3\}$ |
| | Deduces both $x \geq 0$ and $x \neq 3$ with no extras Condone $x > 0$ | 2.2a | A1 | |
| | Obtains correct domain correctly stated in set notation | 2.5 | R1 | |
| Subtotal | | | 3 | |

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|-----------------|--|-----|----------|--|
| 10(b) | States that $h(x)$ has a discontinuity/asymptote at $x = 3$ or in the interval $(1, 4)$ OE | 2.4 | M1 | $h(x)$ is not continuous at $x = 3$ |
| | Explains that the discontinuity is at $x = 3$ and this is in the interval $(1, 4)$ | 2.3 | A1 | This means that a change of sign between $x = 1$ and 4 does not imply a root |
| Subtotal | | | 2 | |

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|-----------------|---|------|----------|---|
| 10(c) | Selects an appropriate method to differentiate and reaches $h'(x)$ of the form $ax^{-\frac{1}{2}}(x-3)^{-1} + bx^{\frac{1}{2}}(x-3)^{-2}$ OE | 3.1a | M1 | $h(x) = \frac{\sqrt{x}}{x-3}$ $h'(x) = \frac{\frac{1}{2}x^{-\frac{1}{2}}(x-3) - x^{\frac{1}{2}}}{(x-3)^2}$ |
| | Obtains correct $h'(x)$ ACF | 1.1b | A1 | |
| | Equates their $h'(x)$ to 0 | 1.1a | M1 | $h'(x) = 0 \Rightarrow \frac{\frac{1}{2}x^{-\frac{1}{2}}(x-3) - x^{\frac{1}{2}}}{(x-3)^2} = 0$ |
| | Obtains $x = -3$ | 1.1b | A1 | $\frac{1}{2}x^{-\frac{1}{2}}(x-3) - x^{\frac{1}{2}} = 0$ |
| | Explains that a continuous function with no turning points is one to one and therefore the inverse exists. Condone omission of 'continuous' | 2.4 | E1 | $\frac{(x-3)}{2\sqrt{x}} - \sqrt{x} = 0$ $x-3-2x=0$ $x=-3$ |
| | Completes a reasoned argument to correctly show that the function is one to one and deduces that $h(x)$ has an inverse Must explain that $x = -3$ is not in the domain and therefore there are no turning points and considers the sign of $h(x)$ either side of $x = 3$ | 2.1 | R1 | $x = -3$ is not in the domain of h hence the function has no turning points $h(x) > 0$ for $x > 3$ $h(x) < 0$ for $x < 3$ Hence function is one to one and has an inverse |
| Subtotal | | | 6 | |

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| | Question Total | | 11 | |
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