

Q	Marking Instructions	AO	Marks	Typical Solution
8(a)	Recalls a correct trig identity, which could lead to a correct answer	AO1.2	B1	(LHS \equiv)
	Demonstrates a strategy for proving the identity, eg by converting all the terms on the LHS to cos and sin.	AO3.1a	M1	$\frac{\sin 2x}{1 + \tan^2 x}$ $\equiv \frac{2 \sin x \cos x}{1 + \tan^2 x}$
	Concludes a rigorous mathematical argument to prove given identity AG	AO2.1	R1	$\equiv \frac{2 \sin x \cos x}{\sec^2 x}$ $\equiv 2 \sin x \cos x \cos^2 x$ $\equiv 2 \sin x \cos^3 x$ (\equiv RHS)
8(b)	Uses identity to write integrand in the form $a \sin 2\theta \cos^3 2\theta$	AO1.1a	M1	$\int \frac{4 \sin 4\theta}{1 + \tan^2 2\theta} d\theta = \int 8 \sin 2\theta \cos^3 2\theta d\theta$
	Correctly writes integrand as $8 \sin 2\theta \cos^3 2\theta$	AO1.1b	A1	Let $u = \cos 2\theta$
	Selects an appropriate method for integrating, e.g. substitution $u = \cos 2\theta$, or by inspection PI by sight of $\cos^4 2\theta$	AO3.1a	M1	then $\frac{du}{d\theta} = -2 \sin 2\theta \Rightarrow \sin 2\theta = -\frac{1}{2} \frac{du}{d\theta}$
	Obtains $k \int u^3 du$ correctly PI by solution in form $k \cos^4 2\theta$, if by inspection	AO1.1a	M1	$I = -4 \int u^3 \frac{du}{d\theta} d\theta$ $= -4 \int u^3 du$ $= -u^4 + c$ $= -\cos^4 2\theta + c$
	Obtains $-u^4$ or $-\cos^4 2\theta$ OE Only FT value of a	AO1.1b	A1F	
	Completes rigorous argument to obtain $-\cos^4 2\theta + c$ OE	AO2.1	R1	
	Total		9	