

Q	Marking instructions	AO	Mark	Typical solution
9(a)	Demonstrates by substitution that $x = 0$ or $y = 0$ leads to value on the LHS = 0	2.4	E1	When $x = 0$ $0^2y^2 + 0y^4 = 0$
	Completes rigorous argument to show required result	2.1	R1	When $y = 0$ $x^20^2 + x0^4 = 0$  This is a contradiction because $x^2y^2 + xy^4 = 12$ so the curve does not intersect either axis
9 (b)(i)	Uses implicit differentiation	3.1a	M1	$2xy^2 + 2x^2y \frac{dy}{dx} + y^4 + 4xy^3 \frac{dy}{dx} = 0$ $\frac{dy}{dx} = -\frac{2xy^2 + y^4}{2x^2y + 4xy^3}$ $= -\frac{y(2xy + y^3)}{y(2x^2 + 4xy^2)}$ $= -\frac{2xy + y^3}{2x^2 + 4xy^2}$
	Product rule used LHS (at least one pair of terms correct)	1.1a	M1	
	Differentiates equation of curve fully correctly	1.1b	A1	
	Collects their $\frac{dy}{dx}$ terms in an equation and factorises	3.1a	M1	
	Completes convincing argument to obtain required result by <b>factorising</b> then simplifying $y$ <b>AG</b>	2.1	R1	
9 (b)(ii)	Begins argument by setting $\frac{dy}{dx} = 0$ to form an equation for $x$ and $y$ <b>PI</b> by $2xy + y^3 = 0$	2.1	M1	For stationary points $\frac{dy}{dx} = 0$ $\Rightarrow 2xy + y^3 = 0$ $\Rightarrow y^2 = -2x$ $\Rightarrow x^2y^2 + x(-2x)y^2 = 12$ $\Rightarrow -x^2y^2 = 12$ Since $-x^2y^2 < 0$ there can be no stationary points.
	Obtains $y^2 = -2x$ or $y = \sqrt{-2x}$ or $x = \frac{-y^2}{2}$	1.1b	A1	
	Substitutes $y^2 = -2x$ or $x = \frac{-y^2}{2}$ into equation for curve	1.1a	M1	
	Completes convincing argument to deduce the required result	2.2a	R1	
9 (b)(iii)	Substitutes $y = 1$ into equation of curve to obtain correct quadratic <b>ACF</b>	3.1a	M1	$y = 1 \Rightarrow x^2 + x - 12 = 0$ $\Rightarrow x = 3 \quad (x > 0)$ $\Rightarrow \frac{dy}{dx} = -\frac{7}{30}$ $y - 1 = -\frac{7}{30}(x - 3)$
	Deduces $x = 3$ <b>PI</b> by substituting their $x$ in their $dy/dx$	2.2a	R1	
	Substitutes their $x$ and $y = 1$ in their $dy/dx$	1.1a	M1	
	Obtains correct equation of tangent <b>ACF</b> <b>ISW</b>	1.1b	A1	
	<b>Total</b>		<b>15</b>	