

Question	Scheme	Marks	AOs
1(a)	$\alpha\left(\frac{5}{\alpha}\right)\left(\alpha + \frac{5}{\alpha} - 1\right) = 15$	M1	1.1b
		A1	1.1b
	$\Rightarrow 5\alpha + \frac{25}{\alpha} - 5 = 15 \Rightarrow \alpha^2 - 4\alpha + 5 = 0$ $\Rightarrow \alpha = \frac{- -4 \pm \sqrt{(-4)^2 - 4(1)(5)}}{2(1)}$ or $(\alpha - 2)^2 - 4 + 5 = 0 \Rightarrow \alpha = \dots$	M1	3.1a
	$\Rightarrow \alpha = 2 \pm i$	A1	1.1b
	Hence the roots of $f(z) = 0$ are $2 + i, 2 - i$ and 3	A1	2.2a
		(5)	
(b)	$p = -\left(“(2 + i)” + “(2 - i)” + “3”\right) \Rightarrow p = \dots$	M1	3.1a
	$\Rightarrow p = -7$ cso	A1	1.1b
		(2)	
	1(b) alternative		
	$f(z) = (z - 3)(z^2 - 4z + 5) \Rightarrow p = \dots$	M1	3.1a
	$\Rightarrow p = -7$ cso	A1	1.1b
		(2)	

(7 marks)

Notes:

(a)

M1: Multiplies the three given roots together and sets the result equal to 15 or -15

A1: Obtains a correct equation in α

M1: Forms a quadratic equation in α and attempts to solve this equation by either completing the square or using the quadratic formula to give $\alpha = \dots$

A1: $\alpha = 2 \pm i$

A1: Deduces the roots are $2 + i, 2 - i$ and 3

(b)

M1: Applies the process of finding $-\sum$ (of their three roots found in part (a)) to give $p = \dots$

A1: $p = -7$ by correct solution only

(b) Alternative

M1: Applies the process expanding $(z - "3")(z - (\text{their sum})z + \text{their product})$ in order to find $p = \dots$

A1: $p = -7$ by correct solution only