

Question	Scheme	Marks	AOs	
4	$\{w = x - 1 \Rightarrow\} x = w + 1$	B1	3.1a	
	$(w+1)^3 + 3(w+1)^2 - 8(w+1) + 6 = 0$	M1	3.1a	
	$w^3 + 3w^2 + 3w + 1 + 3(w^2 + 2w + 1) - 8w - 8 + 6 = 0$			
	$w^3 + 6w^2 + w + 2 = 0$	M1	1.1b	
		A1	1.1b	
		A1	1.1b	
		(5)		
	Alternative			
	$\alpha + \beta + \gamma = -3, \alpha\beta + \beta\gamma + \alpha\gamma = -8, \alpha\beta\gamma = -6$	B1	3.1a	
	sumroots = $\alpha - 1 + \beta - 1 + \gamma - 1$	M1	3.1a	
	$= \alpha + \beta + \gamma - 3 = -3 - 3 = -6$			
	pairsum = $(\alpha - 1)(\beta - 1) + (\alpha - 1)(\gamma - 1) + (\beta - 1)(\gamma - 1)$			
	$= \alpha\beta + \alpha\gamma + \beta\gamma - 2(\alpha + \beta + \gamma) + 3$			
	$= -8 - 2(-3) + 3 = 1$			
product = $(\alpha - 1)(\beta - 1)(\gamma - 1)$				
$= \alpha\beta\gamma - (\alpha\beta + \alpha\gamma + \beta\gamma) + (\alpha + \beta + \gamma) - 1$				
$= -6 - (-8) - 3 - 1 = -2$				
$w^3 + 6w^2 + w + 2 = 0$	M1			1.1b
	A1			1.1b
	A1	1.1b		
	(5)			

(5 marks)

Notes:

B1: Selects the method of making a connection between x and w by writing $x = w + 1$

M1: Applies the process of substituting their $x = w + 1$ into $x^3 + 3x^2 - 8x + 6 = 0$

M1: Depends on previous M mark. Manipulating their equation into the form
 $w^3 + pw^2 + qw + r = 0$

A1: At least two of p, q, r are correct

A1: Correct final equation

Alternative

B1: Selects the method of giving three correct equations each containing α, β and γ

M1: Applies the process of finding sum roots, pair sum and product

M1: Depends on previous M mark. Applies

$$w^3 - (\text{their sum roots})w^2 + (\text{their pair sum})w - \text{their } \alpha\beta\gamma = 0$$

A1: At least two of p, q, r are correct

A1: Correct final equation