

Question	Scheme	Marks	AOs
4.	$(\mathbf{r} =) \begin{pmatrix} -2+\lambda \\ 5-\lambda \\ 4-3\lambda \end{pmatrix} \text{ or } \begin{pmatrix} -2 \\ 5 \\ 4 \end{pmatrix} + \lambda \begin{pmatrix} 1 \\ -1 \\ -3 \end{pmatrix} \text{ (oe)}$	M1	1.1b
	So meet if $\begin{pmatrix} -2+\lambda \\ 5-\lambda \\ 4-3\lambda \end{pmatrix} \cdot \begin{pmatrix} 1 \\ -2 \\ 1 \end{pmatrix} = -7 \Rightarrow (-2+\lambda) \times 1 + (5-\lambda) \times -2 + (4-3\lambda) \times 1 = -7$	M1 A1	3.1a 1.1b
	$\Rightarrow 0\lambda - 8 = -7 \Rightarrow -8 = -7$ a contradiction so no intersection	A1ft	2.3
	Hence l is parallel to Π but not in it.	A1cso	3.2a
		(5)	
(5 marks)			

Notes

- M1** Forms a parametric form for the line. Allow one slip.
- M1** Substitutes into the equation of the plane to an equation in λ . May use Cartesian form of plane to substitute into.
- A1** Correct equation in λ
- A1ft** Simplifies and derives a contradiction and deduces line and plane do not meet. Follow through in their initial equation in λ so
 - contradiction so no intersection if λ disappears and constants unequal
 - line lies in plane if a tautology is arrived at
 - meet in a point if a solution for λ is found.
- But do not allow for incorrect simplification from a correct initial equation in λ**
- Note that a miscopy/misread of 7 instead of -7 can therefore score a maximum of M1M1A0A1A0.
- A1cso** Correct deduction from correct working. This may be seen two separate statements in their working. You may see attempts at showing the line is parallel before/after deducing there is no intersection.

Alt 1

Note that some may attempt a mix of the main scheme and Alt 1. Mark under main scheme unless Alt 1 would score higher.

$\begin{pmatrix} 1 \\ -1 \\ -3 \end{pmatrix} \cdot \begin{pmatrix} 1 \\ -2 \\ 1 \end{pmatrix} = 1 \times 1 + (-1) \times (-2) + (-3) \times 1 = 0$	M1	3.1a
Hence l is parallel to Π	A1	1.1b
$(-2, 5, 4)$ on l , but $(1)(-2) + (-2)(5) + 1(4) = -8$	M1	1.1b
$-8 \neq -7$ so $(-2, 5, 4)$ is not on the plane.	A1ft	2.3
Hence l is (parallel to Π but) not in the plane.	A1cso	3.2a
	(5)	
(5 marks)		

Alt 1 Notes

- M1** Attempts the dot product between the two direction vectors.
- A1** Shows dot product is zero and makes the correct deduction that line is parallel to plane.
- M1** Finds a point on l and substitutes into the equation of Π (vector or Cartesian)
- A1ft** Simplifies and derives a contradiction – follow through their equation, so if arrive at a tautology, they should deduce the line is in the plane.
- A1cso** Correct deduction from correct working but may be split across working.

Question	Scheme	Marks	AOs
Alt 2	Attempts to solve $\frac{x+2}{1} = \frac{y-5}{-1} = \frac{z-4}{-3}$ and $x-2y+z=-7$ simultaneously – eliminates one variable for M mark.	M1	3.1a
	e.g. $y = -(x+2)+5 = -x+3 \Rightarrow x-2(-x+3)+z = -7 \Rightarrow 3x+z = -1$ (oe)	A1	1.1b
	Solves reduced equations, e.g. $-3(x+2) = z-4 \Rightarrow 3x+z = -2$ and $3x+z = -1 \Rightarrow (3x+z) - (3x+z) = -2 - (-1)$	M1	1.1b
	$\Rightarrow 0 = -1$ a contradiction so no intersection	A1ft	2.3
	Hence l is parallel to l_1 but not in it.	A1cso	3.2a
		(5)	

(5 marks)

Alt 2 notes

- M1** Attempts to solve the Cartesian equation of the line and plane, using the plane equation to eliminate one variable for the M.
- A1** Correct elimination of their chosen variable. (E.g may see $3-3y+z = -7$ or $-2x-2y-2 = -7$ etc)
- M1** Solves the reduced equations in two variables...
- A1ft** ... and derives a contradiction/line and plane do not meet. Follow through their result, so may reach a tautology and deduce lies in plane, or find single solution and deduce meet in a point.
- A1cso** Correct deduction from correct working.