

Question	Scheme	Marks	AOs
3	$x^2 + y^2 = r^2$	B1	1.2
	$\{V\} = \pi \int_{-r}^r r^2 - x^2 \, dx$ or $\{V\} = 2\pi \int_0^r r^2 - x^2 \, dx$	B1	2.1
	Integrates to the form $\alpha x \pm \beta x^3$ $\left[\text{note: the correct integration gives } r^2 x - \frac{1}{3} x^3 \right]$	M1	1.1b
	Substitutes limits of $-r$ and r and subtracts the correct way round $\left(r^2(r) - \frac{1}{3}(r)^3 \right) - \left(r^2(-r) - \frac{1}{3}(-r)^3 \right)$ or Substitutes limits of 0 and r and subtracts the correct way round with twice the volume. Note the limit of 0 can be implied if gives and answer of 0 $\left(r^2(r) - \frac{1}{3}(r)^3 \right) - (0)$	dM1	1.1b
	$V = \frac{4}{3} \pi r^3 * \text{cso}$	A1*	1.1b
		(5)	

(5 marks)

Notes:

B1: Correct equation of the circle, may be implied by correct integral

B1: Correct expression for the volume, including limits, dx may be implied and if using limits r and 0 the 2 could appear later with reasoning

M1: Integrates to the form $\alpha x \pm \beta x^3$. Do not award if $r^2 \rightarrow \lambda r^3$

dM1: Dependent on previous method mark. Correct use of limits $-r$ and r or limits of 0 and r with twice the volume.

A1*: $V = \frac{4}{3} \pi r^3 * \text{cso}$

Note: rotation about the y -axis all marks are available, however for the final accuracy mark must refer to symmetry