

Question	Scheme	Marks	AOs
5(a)	Volume = $r \times (r+1) \times (r+2)$	B1	1.1b
	A complete method for finding the total volume of n blocks and expressing it in sigma notation. This can be implied by later work. $\sum_{r=1}^n (r^3 + 3r^2 + 2r)$	M1	3.1b
	$V = \frac{1}{4}n^2(n+1)^2 + 3 \times \frac{1}{6}n(n+1)(2n+1) + 2 \times \frac{n}{2}(n+1)$	M1	2.1
	$V = \frac{1}{4}n(n+1)[n(n+1) + 2(2n+1) + 4]$	dM1	1.1b
	$V = \frac{1}{4}n(n+1)[n^2 + 5n + 6]$ $\Rightarrow V = \frac{1}{4}n(n+1)(n+2)(n+3)^*$	A1*	1.1b
		(5)	
(b)	Sets $\frac{1}{4}n(n+1)(n+2)(n+3) = n^4 + 6n^3 - 11710$ $\frac{1}{4}n^4 + \frac{3}{2}n^3 + \frac{11}{4}n^2 + \frac{3}{2}n = n^4 + 6n^3 - 11710$ simplifies ($3n^4 + 18n^3 - 11n^2 - 6n - 46840 = 0$) and solves $n = \dots$	M1	1.1b
	There are 10 blocks or $n = 10$	A1	3.2a
		(2)	

(7 marks)

Notes:

(a)

B1: Correct volume of a block

M1: Expressing the total volume of all n blocks as a series in terms of r , r^2 and r^3

M1: Substitutes at least one of the standard formulae into their volume.

dM1: Attempts to factorise $\frac{1}{4}n(n+1)$ having used at least one standard formula correctly. Each term must contain a factor of $n(n+1)$

A1*: Obtains the printed result with no errors seen, no bracketing errors and following from

$$V = \frac{1}{4}n(n+1)[n^2 + 5n + 6] \text{ o.e.}$$

Note: Going from $\frac{1}{4}n(n^3 + 6n^2 + 11n + 6)$ to $\frac{1}{4}n(n+1)(n+2)(n+3)$ with no reasoning shown scores **dM0 A0**

(b)

M1: Sets the printed answer $= n^4 + 6n^3 - 11710$, simplifies, collects terms and uses their calculator to solve a quartic equation to find a value for n .

A1: Selects $n = 10$ or states that there are **10 blocks** from a **correct equation**