| $z_{2}=2-3 i$ |
| :--- |
| $\left(z_{3}=\right) p-3 i$ and $\left(z_{4}=\right) p+3 i$ May be seen in an Argand diag |
| $\left(z_{3}=\right)-4-3$ i and $\left(z_{4}=\right)-4+3 i$ May be seen in an Argand |
| diagram, but the complex numbers used in their method takes |
| precedence | | $\left(z^{2}-4 z+13\right)\left(z^{2}+8 z+25\right)$ |
| :--- |
| or |
| $\qquad(z-(2-3 i))(z-(2+3 i))(z-(-4-3 i))(z-(-4+3 i))$ |

or $a=-[(2-3 i)+(2+3 i)+(-4-3 i)+(-4+3 i)]$
and

$$
\begin{aligned}
b & =(2-3 i)(2+3 i)+(2-3 i)(-4-3 i)+(2-3 i)(-4+3 i) \\
& +(2+3 i)(-4-3 i)+(2+3 i)(-4+3 i)+(-4-3 i)(-4+3 i)
\end{aligned}
$$

and

$$
c=-\left[\begin{array}{c}
(2-3 i)(2+3 i)(-4-3 i)+(2-3 i)(2+3 i)(-4+3 i) \\
+(2-3 i)(-4-3 i)(-4+3 i)+(2+3 i)(-4-3 i)(-4+3 i)
\end{array}\right]
$$

and

$$
d=(2-3 i)(2+3 i)(-4-3 i)(-4+3 i)
$$

or
Substitutes in one root from each conjugate pair and equates real and imaginary parts and solves simultaneously

| $(2 \pm 3 \mathrm{i})^{4}+a(2 \pm 3 \mathrm{i})^{3}+b(2 \pm 3 \mathrm{i})^{2}+c(2 \pm 3 \mathrm{i})+d=0$ |  |  |
| :---: | :---: | :---: |
| $(-4 \pm 3 \mathrm{i})^{4}+a(-4 \pm 3 \mathrm{i})^{3}+b(-4 \pm 3 \mathrm{i})^{2}+c(-4 \pm 3 \mathrm{i})+d=0$ |  |  |
| $a=4, b=6, c=4, d=325$ | A 1 | 1.1 b |
| $\mathrm{f}(\mathrm{z})=\mathrm{z}^{4}+4 z^{3}+6 \mathrm{z}^{2}+4 \mathrm{z}+325$ | A 1 | 1.1 b |
|  | (6) |  |

(6 marks)

## Notes:

B1: Seen $2-3 i$
M1: Finds the third and fourth roots of the form $p \pm 3 i$. May be seen in an Argand diagram
A1: Third and fourth roots are $-4 \pm 3$. May be seen in an Argand diagram
dM1: Uses an appropriate method to find $\mathrm{f}(\mathrm{z})$. If using roots of a polynomial at least 3 coefficients must be attempted.
A1: At least two of $a, b, c, d$ correct
A1: All $a, b, c$ and $d$ correct

## Note: Using roots $2 \pm 3 i$ and $-2 \pm 3 i$ leads to $z^{4}+10 z^{2}+169$ Maximum score B1 M1 A0 M1 A0

A0

