

Question	Scheme	Marks	AOs
10	$(x-3)^2 + (y-5)^2 = (2r)^2$ and $y = -x + 2$	B1	1.1b
	$(x-3)^2 + (-x+2-5)^2 = (2r)^2$ or $(-y+2-3)^2 + (y-5)^2 = (2r)^2$	M1	3.1a
	$2x^2 + 18 - 4r^2 = 0$ or $2y^2 - 8y + 26 - 4r^2 = 0$	A1	1.1b
	$b^2 - 4ac > 0 \Rightarrow 0^2 - 4(2)(18 - 4r^2) > 0 \Rightarrow r > \dots$ or $x^2 = 9 - 2r^2 \Rightarrow 9 - 2r^2 > 0 \Rightarrow r > \dots$ or $b^2 - 4ac > 0 \Rightarrow (-8)^2 - 4(2)(26 - 4r^2) > 0 \Rightarrow r > \dots$	dM1	3.1a
	Finds a maximum value for $r$ $(2r)^2 = 5^2 + (3-2)^2 \Rightarrow r = \dots$	M1	3.1a
	$\frac{3\sqrt{2}}{2} < r < \frac{\sqrt{26}}{2}$ o.e.	A1 A1	1.1b 1.1b
	<b>Alternative</b> Using a circle with centre (3, 5) and radius $2r$ and $y = -x + 2$	B1	1.1b
	$y - 5 = 1(x - 3) \Rightarrow y = x + 2$ $x + 2 = -x + 2 \Rightarrow x = \dots$	M1	3.1a
	(0, 2)	A1	1.1b
	$2r > \sqrt{(3-0)^2 + (5-2)^2} \Rightarrow r > \dots$	dM1	3.1a
Finds a maximum value for $r$ $(2r)^2 = 5^2 + (3-2)^2 \Rightarrow r = \dots$	M1	3.1a	
$\frac{3\sqrt{2}}{2} < r < \frac{\sqrt{26}}{2}$ o.e.	A1 A1	1.1b 1.1b	
	(7)		

(7 marks)

**Notes:**

**B1:** Correct equations for each loci of points

**M1:** A complete method to find a 3TQ involving one variable using equations of the form

$$(x \pm 3)^2 + (y \pm 5)^2 = (2r)^2 \text{ or } 2r^2 \text{ or } r^2 \text{ and } y = \pm x \pm 2$$

**A1:** Correct quadratic equation

**dM1:** Dependent on previous method mark. A complete method uses  $b^2 - 4ac > 0$  or rearranges to find  $x^2 = f(r)$  and uses  $f(r) > 0$  to the minimum value of  $r$ .

**M1:** Realises there will be an upper limit for  $r$  and uses Pythagoras theorem

$$(2r)^2 = (\text{y coord of centre})^2 + (\text{x coord of centre} - 2)^2$$

$$\text{condone } (r)^2 = (\text{y coord of centre})^2 + (\text{x coord of centre} - 2)^2$$

**A1:** One correct limit, either  $\frac{3\sqrt{2}}{2} < r$  or  $r < \frac{\sqrt{26}}{2}$  o.e.

**A1:** Fully correct inequality

### Alternative

**B1:** Using a circle with centre  $(3, 5)$  and radius  $2r$  and  $y = -x + 2$

**M1:** A complete method to find the point of intersection of the line  $y = \pm x \pm 2$  and circle where the line is a tangent to the circle.

**A1:** Correct point of intersection

**dM1:** Finds the distance between the point of intersection and the centre and uses this to find the minimum value of  $r$ . Condone radius of  $r$ .

**M1:** Realises there will be an upper limit for  $r$  and uses Pythagoras theorem

$$(2r)^2 = (\text{y coord of centre})^2 + (\text{x coord of centre} - 2)^2$$

**A1:** One correct limit, either  $\frac{3\sqrt{2}}{2} < r$  or  $r < \frac{\sqrt{26}}{2}$  o.e.

**A1:** Fully correct inequality