

| Question            | Scheme   | Marks           | AOs                  |
|---------------------|--|-----------------|----------------------|
| 2                   | $w = 3x - 2 \Rightarrow x = \frac{w+2}{3}$   | B1              | 3.1a                 |
|                     | $9\left(\frac{w+2}{3}\right)^3 - 5\left(\frac{w+2}{3}\right)^2 + 4\left(\frac{w+2}{3}\right) + 7 = 0$                                | M1              | 3.1a                 |
|                     | $\frac{1}{3}(w^3 + 6w^2 + 12w + 8) - \frac{5}{9}(w^2 + 4w + 4) + \frac{4}{3}(w + 2) + 7 = 0$   |                 |                      |
|                     | $3w^3 + 13w^2 + 28w + 91 = 0$  | dM1<br>A1<br>A1 | 1.1b<br>1.1b<br>1.1b |
|                     |  | (5)             |                      |
| <b>Alternative:</b> |  |                 |                      |
|                     | $\alpha + \beta + \gamma = \frac{5}{9}, \alpha\beta + \beta\gamma + \alpha\gamma = \frac{4}{9}, \alpha\beta\gamma = -\frac{7}{9}$    | B1              | 3.1a                 |
|                     | New sum = $3(\alpha + \beta + \gamma) - 6 = -\frac{13}{3}$   | M1              | 3.1a                 |
|                     | New pair sum = $9(\alpha\beta + \beta\gamma + \gamma\alpha) - 12(\alpha + \beta + \gamma) + 12 = \frac{28}{3}$                       |                 |                      |
|                     | New product = $27\alpha\beta\gamma - 18(\alpha\beta + \beta\gamma + \gamma\alpha) + 12(\alpha + \beta + \gamma) - 8 = -\frac{91}{3}$ |                 |                      |
|                     | $w^3 - \left(-\frac{13}{3}\right)w^2 + \frac{28}{3}w - \left(-\frac{91}{3}\right) = 0$   | dM1             | 1.1b                 |
|                     | $3w^3 + 13w^2 + 28w + 91 = 0$  | A1<br>A1        | 1.1b<br>1.1b         |
|                     |  | (5)             |                      |

**(5 marks)**

### Notes

B1: Selects the method of making a connection between  $x$  and  $w$  by writing  $x = \frac{w+2}{3}$

Condone the use of a different letter than  $w$

M1: Applies the process of substituting  $x = \frac{w+2}{3}$  into  $9x^3 - 5x^2 + 4x + 7 = 0$

dM1: Depends on the previous M mark. Manipulates their equation into the form  $aw^3 + bw^2 + cw + d (= 0)$ . Condone the use of a different letter than  $w$  consistent with B1 mark.

A1: At least two of  $a, b, c, d$  correct

A1: Fully correct equation, must be in terms of  $w$

#### **Alternative:**

B1: Selects the method of giving three correct equations containing  $\alpha, \beta$  and  $\gamma$

M1: Applies the process of finding the new sum, new pair sum, new product

dM1: Depends on the previous M mark. Applies

$w^3 - (\text{new sum})w^2 + (\text{new pair sum})w - (\text{new product}) (= 0)$  condone the use of any letter here.

A1: At least two of  $a, b, c, d$  correct

A1: Fully correct equation in term of  $w$