

Question	Scheme	Marks	AOs
14	$y = (x-2)^2(x+3) = (x^2 - 4x + 4)(x+3) = x^3 - 1x^2 - 8x + 12$	B1	1.1b
	An attempt to find $x$ coordinate of the maximum point. To score this you must see either <ul style="list-style-type: none"> <li>an attempt to expand <math>(x-2)^2(x+3)</math>, an attempt to differentiate the result, followed by an attempt at solving <math>\frac{dy}{dx} = 0</math></li> <li>an attempt to differentiate <math>(x-2)^2(x+3)</math> by the product rule followed by an attempt at solving <math>\frac{dy}{dx} = 0</math></li> </ul>	M1	3.1a
	$y = x^3 - 1x^2 - 8x + 12 \Rightarrow \frac{dy}{dx} = 3x^2 - 2x - 8$	M1	1.1b
	Maximum point occurs when $\frac{dy}{dx} = 0 \Rightarrow (x-2)(3x+4) = 0$ $\Rightarrow x = -\frac{4}{3}$	M1 A1	1.1b 1.1b
	An attempt to find the area under $y = (x-2)^2(x+3)$ between two values. To score this you must see an attempt to expand $(x-2)^2(x+3)$ followed by an attempt at using two limits	M1	3.1a
	Area = $\int (x^3 - 1x^2 - 8x + 12)dx = \left[ \frac{x^4}{4} - \frac{x^3}{3} - 4x^2 + 12x \right]$	M1	1.1b
	Uses a top limit of 2 and a bottom limit of their $x = -\frac{4}{3} R = \left[ \frac{x^4}{4} - \frac{x^3}{3} - 4x^2 + 12x \right]_{-\frac{4}{3}}^2$	M1	2.2a
	Uses = $\frac{28}{3} - -\frac{1744}{81} = \frac{2500}{81}$	A1	2.1
		(9)	

(9 marks)

**Notes:**

**B1:** Expands  $(x-2)^2(x+3)$  to  $x^3 - 1x^2 - 8x + 12$  seen at some point in their solution. It may appear just on their integral for example.

**M1:** This is a problem solving mark for knowing the method of finding the maximum point. You should expect to see the key points used (i) differentiation (ii) solution of their  $\frac{dy}{dx} = 0$

**M1:** For correctly differentiating their cubic with at least two terms correct (for their cubic).

**M1:** For setting their  $\frac{dy}{dx} = 0$  and solves using a correct method (including calculator methods)

**A1:**  $\Rightarrow x = -\frac{4}{3}$

**M1:** This is a problem solving mark for knowing how integration is used to find the area underneath a curve between two points.

**M1:** For correctly integrating their cubic with at least two correct terms (for their cubic).

**M1:** For deducing the top limit is 2, the bottom limit is their  $x = -\frac{4}{3}$  and applying these correctly within their integration.

**A1:** Shows above steps clearly and proceeds to  $R = \frac{2500}{81}$