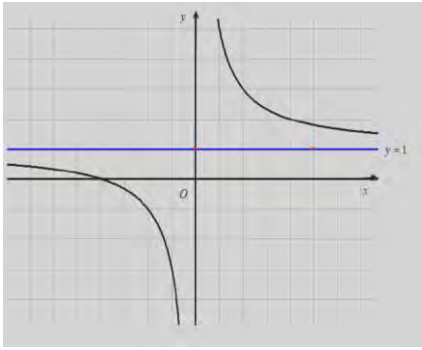


Question	Scheme	Marks	AOs
7 (a)	 <p><math>\frac{1}{x}</math> shape in 1st quadrant</p> <p>Correct</p> <p>Asymptote <math>y = 1</math></p>	M1	1.1b
		A1	1.1b
		B1	1.2
		(3)	
(b)	Combines equations $\Rightarrow \frac{k^2}{x} + 1 = -2x + 5$	M1	1.1b
	$(\times x) \Rightarrow k^2 + 1x = -2x^2 + 5x \Rightarrow 2x^2 - 4x + k^2 = 0^*$	A1*	2.1
		(2)	
(c)	Attempts to set $b^2 - 4ac = 0$	M1	3.1a
	$8k^2 = 16$	A1	1.1b
	$k = \pm\sqrt{2}$	A1	1.1b
		(3)	

(8 marks)

### Notes

(a)

**M1:** For the shape of a  $\frac{1}{x}$  type curve in Quadrant 1. It must not cross either axis and have acceptable curvature. Look for a negative gradient changing from  $-\infty$  to 0 condoning "slips of the pencil". (See Practice and Qualification for clarification)

**A1:** Correct shape and position for both branches.

It must lie in Quadrants 1, 2 and 3 and have the correct curvature including asymptotic behaviour

**B1:** Asymptote given as  $y = 1$ . This could appear on the diagram or within the text.

Note that the curve does not need to be asymptotic at  $y = 1$  but this must be the only horizontal asymptote offered by the candidate.

(b)

**M1:** Attempts to combine  $y = \frac{k^2}{x} + 1$  with  $y = -2x + 5$  to form an equation in just  $x$

**A1\*:** Multiplies by  $x$  (the processed line must be seen) and proceeds to given answer with no slips.

Condone if the order of the terms are different  $2x^2 + k^2 - 4x = 0$

(c)

**M1:** Deduces that  $b^2 - 4ac = 0$  or equivalent for **the given equation**.

If  $a, b$  and  $c$  are stated only accept  $a = 2, b = \pm 4, c = k^2$  so  $4^2 - 4 \times 2 \times k^2 = 0$

Alternatively completes the square  $x^2 - 2x + \frac{1}{2}k^2 = 0 \Rightarrow (x-1)^2 = 1 - \frac{1}{2}k^2 \Rightarrow "1 - \frac{1}{2}k^2" = 0$

**A1:**  $8k^2 = 16$  or exact simplified equivalent. Eg  $8k^2 - 16 = 0$

If  $a$ ,  $b$  and  $c$  are stated they must be correct. Note that  $b^2$  appearing as  $4^2$  is correct

Note on Question 7 continue

**A1:**  $k = \pm\sqrt{2}$  and following correct  $a$ ,  $b$  and  $c$  if stated

A solution via differentiation would be awarded as follows

**M1:** Sets the gradient of the curve  $= -2 \Rightarrow -\frac{k^2}{x^2} = -2 \Rightarrow x = (\pm)\frac{k}{\sqrt{2}}$  oe and attempts to

substitute into  $2x^2 - 4x + k^2 = 0$

**A1:**  $2k^2 = (\pm)2\sqrt{2}k$  oe

**A1:**  $k = \pm\sqrt{2}$