

Question	Scheme	Marks	AOs
<b>12(a)</b>	$\frac{10\sin^2 \theta - 7\cos \theta + 2}{3 + 2\cos \theta} \equiv \frac{10(1 - \cos^2 \theta) - 7\cos \theta + 2}{3 + 2\cos \theta}$	M1	1.1b
	$\equiv \frac{12 - 7\cos \theta - 10\cos^2 \theta}{3 + 2\cos \theta}$	A1	1.1b
	$\equiv \frac{(3 + 2\cos \theta)(4 - 5\cos \theta)}{3 + 2\cos \theta}$	M1	1.1b
	$\equiv 4 - 5\cos \theta *$	A1*	2.1
		<b>(4)</b>	
<b>(b)</b>	$4 + 3\sin x = 4 - 5\cos x \Rightarrow \tan x = -\frac{5}{3}$	M1	2.1
	$x = \text{awrt } 121^\circ, 301^\circ$	A1 A1	1.1b 1.1b
		<b>(3)</b>	

**(7 marks)**

### Notes

**(a)**

**M1:** Uses the identity  $\sin^2 \theta = 1 - \cos^2 \theta$  within the fraction

**A1:** Correct (simplified) expression in just  $\cos \theta$   $\frac{12 - 7\cos \theta - 10\cos^2 \theta}{3 + 2\cos \theta}$  or exact equivalent such

as  $\frac{(3 + 2\cos \theta)(4 - 5\cos \theta)}{3 + 2\cos \theta}$  Allow for  $\frac{12 - 7u - 10u^2}{3 + 2u}$  where they introduce  $u = \cos \theta$

We would condone mixed variables here.

**M1:** A correct attempt to factorise the numerator, usual rules. Allow candidates to use  $u = \cos \theta$  oe

**A1\*:** A fully correct proof with correct notation and no errors.

Only withhold the last mark for (1) Mixed variable e.g.  $\theta$  and  $x$ 's (2) Poor notation

$\cos \theta^2 \leftrightarrow \cos^2 \theta$  or  $\sin^2 = 1 - \cos^2$  within the solution.

Don't penalise incomplete lines if it is obvious that it is just part of their working

E.g. 
$$\frac{10\sin^2 \theta - 7\cos \theta + 2}{3 + 2\cos \theta} \equiv \frac{10(1 - \cos^2 \theta) - 7\cos \theta + 2}{3 + 2\cos \theta} = \frac{12 - 7\cos \theta - 10\cos^2 \theta}{3 + 2\cos \theta}$$

**(b)**

**M1:** Attempts to use part (a) and proceeds to an equation of the form  $\tan x = k$ ,  $k \neq 0$

Condone  $\theta \leftrightarrow x$  Do not condone  $a \tan x = 0 \Rightarrow \tan x = b \Rightarrow x = \dots$

Alternatively squares  $3\sin x = -5\cos x$  and uses  $\sin^2 x = 1 - \cos^2 x$  oe to reach

$\sin x = A, -1 < A < 1$  or  $\cos x = B, -1 < B < 1$

**A1:** Either  $x = \text{awrt } 121^\circ$  **or**  $301^\circ$ . Condone awrt 2.11 or 5.25 which are the radian solutions

**A1:** Both  $x = \text{awrt } 121^\circ$  **and**  $301^\circ$  and no other solutions.

Answers without working, or with no incorrect working in (b).

Question states hence or otherwise so allow

For 3 marks both  $x = \text{awrt } 121^\circ$  **and**  $301^\circ$  and no other solutions.

For 1 marks scored SC 100 for either  $x = \text{awrt } 121^\circ$  **or**  $301^\circ$

Notes on Question 12 continue

Alternative proof in part (a):

**M1:** Multiplies across and form 3TQ in  $\cos \theta$  on rhs

$$10\sin^2 \theta - 7\cos \theta + 2 = (4 - 5\cos \theta)(3 + 2\cos \theta) \Rightarrow 10\sin^2 \theta - 7\cos \theta + 2 = A\cos^2 \theta + B\cos \theta + C$$

**A1:** Correct identity formed  $10\sin^2 \theta - 7\cos \theta + 2 = -10\cos^2 \theta - 7\cos \theta + 12$

**dM1:** Uses  $\cos^2 \theta = 1 - \sin^2 \theta$  on the rhs or  $\sin^2 \theta = 1 - \cos^2 \theta$  on the lhs

Alternatively proceeds to  $10\sin^2 \theta + 10\cos^2 \theta = 10$  and makes a statement about

$$\sin^2 \theta + \cos^2 \theta = 1 \text{ oe}$$

**A1\*:** Shows that  $(4 - 5\cos \theta)(3 + 2\cos \theta) \equiv 10\sin^2 \theta - 7\cos \theta + 2$  oe AND makes a minimal statement "hence true"