

Question	Scheme	Marks	AOs
10 (a)	$g(5) = 2 \times 5^3 + 5^2 - 41 \times 5 - 70 = \dots$	M1	1.1a
	$g(5) = 0 \Rightarrow (x - 5)$ is a factor, hence $g(x)$ is divisible by $(x - 5)$.	A1	2.4
		(2)	
(b)	$2x^3 + x^2 - 41x - 70 = (x - 5)(2x^2 \dots x \pm 14)$	M1	1.1b
	$= (x - 5)(2x^2 + 11x + 14)$	A1	1.1b
	Attempts to factorise quadratic factor	dM1	1.1b
	$(g(x)) = (x - 5)(2x + 7)(x + 2)$	A1	1.1b
		(4)	
(c)	$\int 2x^3 + x^2 - 41x - 70 \, dx = \frac{1}{2}x^4 + \frac{1}{3}x^3 - \frac{41}{2}x^2 - 70x$	M1 A1	1.1b 1.1b
	Deduces the need to use $\int_{-2}^5 g(x) dx$ $-\frac{1525}{3} - \frac{190}{3}$	M1	2.2a
	Area = $571\frac{2}{3}$	A1	2.1
		(4)	
	(10 marks)		

Notes

- (a)

M1: Attempts to calculate $g(5)$ Attempted division by $(x - 5)$ is M0
Look for evidence of embedded values or two correct terms of $g(5) = 250 + 25 - 205 - 70 = \dots$

A1: Correct calculation, reason and conclusion. It must follow M1. Accept, for example, $g(5) = 0 \Rightarrow (x - 5)$ is a factor, hence divisible by $(x - 5)$
 $g(5) = 0 \Rightarrow (x - 5)$ is a factor ✓
Do not allow if candidate states $f(5) = 0 \Rightarrow (x - 5)$ is a factor, hence divisible by $(x - 5)$ (It is not f)
 $g(x) = 0 \Rightarrow (x - 5)$ is a factor (It is not g(x) and there is no conclusion)
This may be seen in a preamble before finding $g(5) = 0$ but in these cases there must be a minimal statement ie QED, "proved", tick etc.
- (b)

M1: Attempts to find the quadratic factor by inspection (correct coefficients of first term and $\pm$ last term) or by division (correct coefficients of first term and $\pm$ second term). Allow this to be scored from division in part (a)

A1: $(2x^2 + 11x + 14)$ You may not see the $(x - 5)$ which can be condoned

dM1: Correct attempt to factorise their $(2x^2 + 11x + 14)$

A1: $(g(x) = (x-5)(2x+7)(x+2) \text{ or } (g(x) = (x-5)(x+3.5)(2x+4)$

It is for the product of factors and not just a statement of the three factors

Attempts with calculators via the three roots are likely to score 0 marks. The question was "Hence" so the two M's must be awarded.

(c)

M1: For $x^n \rightarrow x^{n+1}$ for any of the terms in x for $g(x)$ so

$$2x^3 \rightarrow \dots x^4, x^2 \rightarrow \dots x^3, -41x \rightarrow \dots x^2, -70 \rightarrow \dots x$$

A1: $\int 2x^3 + x^2 - 41x - 70 \, dx = \frac{1}{2}x^4 + \frac{1}{3}x^3 - \frac{41}{2}x^2 - 70x$ which may be left unsimplified (ignore any reference to $+C$)

M1: Deduces the need to use $\int_{-2}^5 g(x) \, dx$.

This may be awarded from the limits on their integral (either way round) or from embedded values which can be subtracted either way round.

A1: For clear work showing all algebraic steps leading to $\text{area} = 571\frac{2}{3}$ oe

So allow $\int_{-2}^5 2x^3 + x^2 - 41x - 70 \, dx = \left[\frac{1}{2}x^4 + \frac{1}{3}x^3 - \frac{41}{2}x^2 - 70x \right]_{-2}^5 = -\frac{1715}{3} \Rightarrow \text{area} = \frac{1715}{3}$
for 4 marks

Condone spurious notation, as long as the algebraic steps are correct. If they find $\int_{-2}^5 g(x) \, dx$

then withhold the final mark if they just write a positive value to this integral since

$$\int_{-2}^5 g(x) \, dx = -\frac{1715}{3}$$

Note $\int_{-2}^5 2x^3 + x^2 - 41x - 70 \, dx \Rightarrow \frac{1715}{3}$ with no algebraic integration seen scores M0A0M1A0