

8. The temperature,  $\theta^\circ\text{C}$ , of a cup of tea  $t$  minutes after it was placed on a table in a room, is modelled by the equation

$$\theta = 18 + 65e^{-\frac{t}{8}} \quad t \geq 0$$

Find, according to the model,

- (a) the temperature of the cup of tea when it was placed on the table, (1)
- (b) the value of  $t$ , to one decimal place, when the temperature of the cup of tea was  $35^\circ\text{C}$ . (3)
- (c) Explain why, according to this model, the temperature of the cup of tea could not fall to  $15^\circ\text{C}$ . (1)

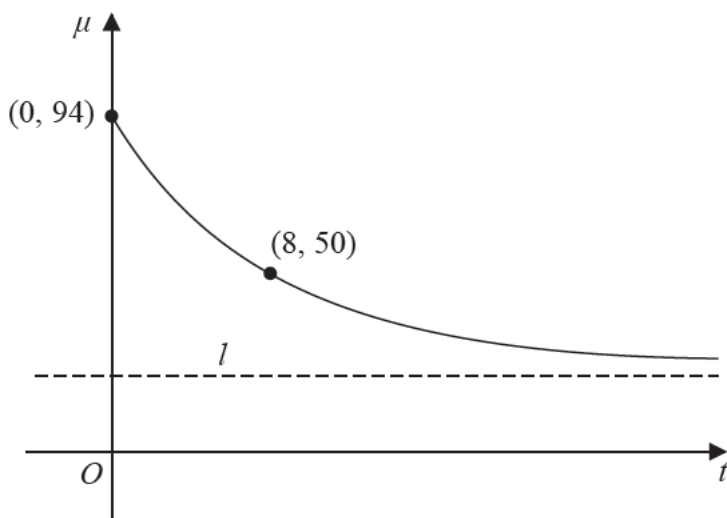


Figure 2

The temperature,  $\mu^\circ\text{C}$ , of a second cup of tea  $t$  minutes after it was placed on a table in a different room, is modelled by the equation

$$\mu = A + Be^{-\frac{t}{8}} \quad t \geq 0$$

where  $A$  and  $B$  are constants.

Figure 2 shows a sketch of  $\mu$  against  $t$  with two data points that lie on the curve.

The line  $l$ , also shown on Figure 2, is the asymptote to the curve.

Using the equation of this model and the information given in Figure 2

- (d) find an equation for the asymptote  $l$ . (4)