

Question	Scheme	Marks	AOs
<b>13 (a)</b>	Substitutes $t = 8 \Rightarrow N = 65 - 3e^{0.8} = (58.32)$	M1	3.4
	Reduction in level of nitrate in first 8 hours = $62 - 58.32$	dM1	3.1b
	$= 3.68$ (ppm)	A1	1.1b
		<b>(3)</b>	
<b>(b)</b>	Substitutes $N = 20 \Rightarrow 20 = 65 - 3e^{0.1t} \Rightarrow 3e^{0.1t} = 45$	M1	3.4
	Correct use of ln's $\Rightarrow 0.1t = \ln(15) \Rightarrow t = \dots$	dM1	1.1b
	$t =$ awrt 27.1 hours	A1	1.1b
		<b>(3)</b>	
<b>(c)</b>	Any valid limitation e.g. <ul style="list-style-type: none"> <li>• If it rains then the concentration will be reduced naturally</li> <li>• The treatment might not be uniform throughout the pond so the fish may not be safe in some areas of the pond even after 27.1 hours</li> <li>• When <math>t &gt; 30.76</math> the concentration becomes negative which cannot happen</li> <li>• The model predicts negative concentration levels for certain values of <math>t</math>. E.g. <math>t = 40 \Rightarrow N \approx -99</math> ppm</li> </ul>	B1	3.5b
		<b>(1)</b>	
			<b>(7 marks)</b>
<b>Notes:</b>			

**(a)**  
**M1:** Substitutes  $t = 8 \Rightarrow N = 65 - 3e^{0.8} = (58.3)$

**dM1:** Attempts  $N_{t=8} - N_{t=0}$  but accept  $N_{t=0} - N_{t=8}$

**A1:** Awrt 3.68 (ppm)

**(b)**  
**M1:** Substitutes  $N = 20$  and proceeds to a form  $Pe^{0.1t} = Q$

**dM1:** Uses correct ln work and proceeds to a value for  $t$ .

**A1:** For awrt 27.1 (hours)

**(c)**  
**B1:** For stating any valid limitation of the model

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Solutions in (b) via trial and improvement or other numerical methods.

Any correct answer following a solution not involving lns can be awarded SC 100

E.g.  $N = 20 \Rightarrow 20 = 65 - 3e^{0.1t} \Rightarrow 3e^{0.1t} = 45 \Rightarrow t = 27.1$