

Question	Scheme	Marks	AOs
<b>15 (a)</b>	$y = \frac{3x}{2} + 32x^{-\frac{3}{2}} \Rightarrow \frac{dy}{dx} = \frac{3}{2} - 48x^{-\frac{5}{2}}$	M1 A1	1.1b 1.1b
	Substitute $x = 4 \Rightarrow \frac{dy}{dx} = \frac{3}{2} - 48 \times 4^{-\frac{5}{2}}$	M1	1.1b
	$\frac{dy}{dx} = \frac{3}{2} - 48 \times \frac{1}{32} = 0 \Rightarrow$ stationary point at $x = 4$ *	A1*	2.1
		<b>(4)</b>	
<b>(b)</b>	$\int \left( \frac{3x}{2} + 32x^{-\frac{3}{2}} \right) dx = \frac{3x^2}{4} - 64x^{-\frac{1}{2}}$	M1 A1	1.1b 1.1b
	States or uses $y = 10$ as the equation for $l$	B1	1.1b
	Area $R = \left[ \frac{3x^2}{4} - 64x^{-\frac{1}{2}} \right]_4^8 - 4 \times y_{x=4}$	dM1	3.1a
	$= 28 - 16\sqrt{2}$	A1	1.1b
		<b>(5)</b>	
			<b>(9 marks)</b>
<b>Notes:</b>			

**(a)**

**M1:** Attempts to differentiate. Look for either  $\frac{3x}{2} \rightarrow \frac{3}{2}$  or  $x^{-\frac{3}{2}} \rightarrow x^{-\frac{5}{2}}$

Condone unprocessed terms for this mark

**A1:** Correct differentiation. This may be left unsimplified

**M1:** Either substitutes  $x = 4$  into their  $\frac{dy}{dx}$  and finds its value

Or alternatively attempts to solve  $\frac{dy}{dx} = 0$

**A1\*:** Complete proof showing that the stationary point is at  $x = 4$

This requires (1) correct differentiation (2) correct calculations shown (see scheme) (3) reason given

**(b)**

**M1:** Attempts to integrate. Look for one correct index (which may be left unprocessed)

If they attempt  $\int (y_1 - y_2) dx$  where  $y_2 = "10"$  just consider  $\int y_1 dx$

**A1:** Correct integration which may be left unsimplified. No requirement for  $+ c$

**B1:** States or uses  $y = 10$  as the equation for  $l$ . This is implied by sight of  $4 \times 10$  in area calculation

**dM1:** Full method to find area for  $R$ .

See scheme but may also be scored for  $\left[ \frac{3x^2}{4} - 64x^{-\frac{1}{2}} - 10x \right]_4^8$

**A1:**  $28 - 16\sqrt{2}$