

10.

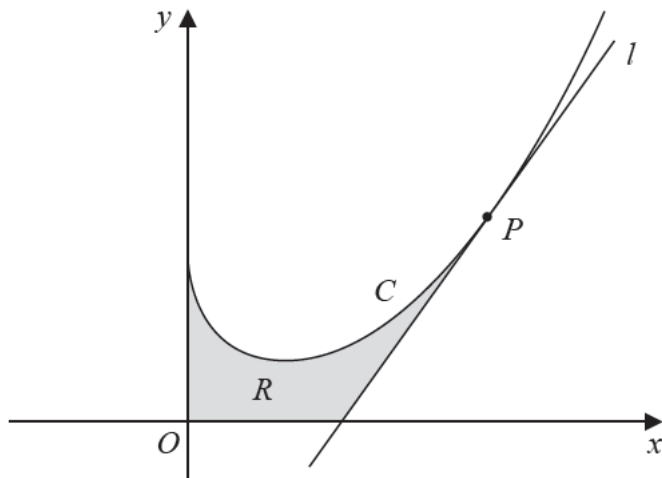


Figure 2

**In this question you must show all stages of your working.**

**Solutions relying on calculator technology are not acceptable.**

Figure 2 shows a sketch of part of the curve  $C$  with equation

$$y = \frac{1}{3}x^2 - 2\sqrt{x} + 3 \quad x \geq 0$$

The point  $P$  lies on  $C$  and has  $x$  coordinate 4

The line  $l$  is the tangent to  $C$  at  $P$ .

(a) Show that  $l$  has equation

$$13x - 6y - 26 = 0$$

(5)

The region  $R$ , shown shaded in Figure 2, is bounded by the  $y$ -axis, the curve  $C$ , the line  $l$  and the  $x$ -axis.

(b) Find the exact area of  $R$ .

(5)