

| Question | Scheme | Marks | AOs |
|-------------|---|----------|--------------|
| 3(a) | $y = 4x - 3x^{\frac{3}{2}} + 13, \quad y = 13 - 2x, \quad A(4, 5)$ | | |
| | $y = 4(4) - 3(4)^{\frac{3}{2}} + 13 = 5$ and $y = 13 - 2(4) = 5$ | M1 | 1.1b |
| | The curve and the line intersect at $(4, 5)$ * | A1* | 2.1 |
| | | (2) | |
| (b) | $\int 4x - 3x^{\frac{3}{2}} + 13 dx = 2x^2 - \frac{6}{5}x^{\frac{5}{2}} + 13x (+c)$ | M1 A1 | 1.1b 1.1b |
| | $\left[2x^2 - \frac{6}{5}x^{\frac{5}{2}} + 13x \right]_0^4 - \frac{1}{2} \times 4(13+5)$ $= \frac{228}{5} - 36$ | dM1 | 3.1a |
| | Area of $R = 9.6$ | A1 | 1.1b |
| | | (4) | |

(b) Alternative

| | | | |
|--|---|----------|--------------|
| | $\int 4x - 3x^{\frac{3}{2}} + 13 - (13 - 2x) dx = 3x^2 - \frac{6}{5}x^{\frac{5}{2}} (+c)$ | M1 A1 | 1.1b 1.1b |
| | $\left[3x^2 - \frac{6}{5}x^{\frac{5}{2}} \right]_0^4 = 3(4)^2 - \frac{6}{5}(4)^{\frac{5}{2}} (-0)$ | dM1 | 3.1a |
| | Area of $R = 9.6$ | A1 | 1.1b |

(6 marks)

Notes:

(a) M1: Attempts to substitute $x = 4$ into both $y = 4x - 3x^{\frac{3}{2}} + 13$ and $y = 13 - 2x$.

Alternatively, sets $4x - 3x^{\frac{3}{2}} + 13 = 13 - 2x$, solves, and substitutes $x = 4$ into either equation for y

A1*: Obtains $y = 5$ for both and concludes that the curve and line intersect at $(4, 5)$.

In the alternative, solves $4x - 3x^{\frac{3}{2}} + 13 = 13 - 2x$ using correct algebra to achieve $x = 4$ and substitutes into either equation for y to achieve $y = 5$ and concludes that the curve and line intersect at $(4, 5)$.

(b)

M1: For an attempt to integrate $x^n \rightarrow x^{n+1}$ for C in at least one term.

A1: Correct integration.

dM1: For the key step in achieving a fully correct strategy for the area, e.g., attempts the trapezium and subtracts from the area enclosed between the curve, the x -axis, the y -axis and $x = 4$.

(Condone the omission of the “- 0”)

A1: 9.6 o.e. e.g., $\frac{48}{5}$

(b) Alternative

M1: For an attempt to integrate $x^n \rightarrow x^{n+1}$ for “ $C - l$ ” in at least one term.

A1: Correct integration.

dM1: For the key step in achieving a fully correct strategy for the area. (Condone the omission of the “ $- 0$ ”)

A1: 9.6 o.e. e.g., $\frac{48}{5}$