

Question	Scheme	Marks	AOs
9(a)	$5 \cos \theta = 24 \tan \theta$		
	Attempts to use both $\tan \theta = \frac{\sin \theta}{\cos \theta}$ and $\sin^2 \theta + \cos^2 \theta = 1$ and arrives at a quadratic equation in $\sin \theta$	M1	3.1a
	$5 \cos \theta = 24 \tan \theta \Rightarrow 5 \cos^2 \theta = 24 \sin \theta$	B1	1.1b
	$5(1 - \sin^2 \theta) = 24 \sin \theta \Rightarrow 5 - 5 \sin^2 \theta = 24 \sin \theta$	M1	1.1b
	Arrives at $5 \sin^2 \theta + 24 \sin \theta - 5 = 0$ with no errors. *	A1*	2.1
		(4)	
(b)	$(5 \sin x - 1)(\sin x + 5) = 0 \Rightarrow \sin x = \dots \Rightarrow x = \dots$	M1	1.1b
	Any one of $x = 11.5^\circ, 168.5^\circ, 371.5^\circ, 528.5^\circ$	A1	1.1b
	$x = 11.5^\circ, 168.5^\circ, 371.5^\circ, 528.5^\circ$ only	A1	2.2a
		(3)	
(c)	Deduces that there are 8 times as many solutions in the interval. $8 \times "4" = 32$	B1ft	2.2a
		(1)	

(8 marks)

Notes:

(a)

M1: An overall problem-solving mark, condoning slips, for an attempt to

- Use $\tan \theta = \frac{\sin \theta}{\cos \theta}$
- Use $\pm \sin^2 \theta \pm \cos^2 \theta = \pm 1$
- Arrive at a quadratic equation in $\sin \theta$

B1: Uses the correct identity and multiplies across to give $5 \cos \theta = 24 \tan \theta \Rightarrow 5 \cos^2 \theta = 24 \sin \theta$

M1: Uses the correct identity $\sin^2 \theta + \cos^2 \theta = 1$ to form a quadratic in $\sin \theta$

A1*: Arrives at the given answer $5 \sin^2 \theta + 24 \sin \theta - 5 = 0$ with no errors.

(b)

M1: Attempts to solve the given quadratic in $\sin x$ using an appropriate method (it is acceptable to use a calculator to solve this) and proceeds to at least one value of x

A1: At least one correct value of x

A1: $x = 11.5^\circ, 168.5^\circ, 371.5^\circ, 528.5^\circ$ only in the given interval. Ignore solutions outside the interval. Do not penalise missing degree symbols.

(c)

B1ft: $8 \times$ their number of solutions to part (b). Allow a restart – so 32 is accepted regardless of their answer in (b).