

Question	Scheme	Marks	AOs
1	$\frac{2\sqrt{x}}{x^2} \rightarrow \dots x^{-\frac{3}{2}} \text{ or } \frac{-3}{x^2} \rightarrow \dots x^{-2}$	M1	1.1b
	$\int \frac{2\sqrt{x}-3}{x^2} dx = \int 2x^{-\frac{3}{2}} - 3x^{-2} dx$	A1	1.1b
	$\dots x^{-\frac{3}{2}} \rightarrow \dots x^{-\frac{1}{2}} \text{ or } \dots x^{-2} \rightarrow \dots x^{-1}$	dM1	1.1b
	$\int 2x^{-\frac{3}{2}} - 3x^{-2} dx = -4x^{-\frac{1}{2}} + 3x^{-1} + c$	A1	1.1b
		(4)	

(4 marks)

### Notes

M1: For separating the fraction into two separate terms. Award for one correct index (which does not need to be processed. e.g.  $\dots x^{\frac{1}{2}-2}$ )

Note  $-\frac{3}{x^2}$  is insufficient. They must write as  $\dots x^{-2}$  or may be implied by further work.

Beware of candidates who integrate the numerator and denominator which results in a correct index but is an incorrect method and scores M0A0dM0A0

A1:  $2x^{-\frac{3}{2}} - 3x^{-2}$  o.e. where the indices have been processed (may be implied by further work)

dM1: For raising the power by one on at least one term with a correct index. It is dependent on the previous method mark. The index does not need to be processed. e.g.  $\dots x^{-\frac{3}{2}} \rightarrow \dots x^{-\frac{3}{2}+1}$ . It is not for  $+c$ .

A1: All correct, simplified and on one line including  $+c$ . Allow other simplified equivalent terms such eg.  $-\frac{4}{\sqrt{x}}$  for  $-4x^{-\frac{1}{2}}$  or e.g.  $\frac{3}{x}$  for  $3x^{-1}$  but do not allow e.g.  $+ -4x^{-\frac{1}{2}}$  or

$$-\frac{4}{1}x^{-\frac{1}{2}}$$

Award once a correct expression is seen and is w but if there is any additional/incorrect notation and no correct expression has been seen on its own, withhold the final mark.

e.g.  $\int -4x^{-\frac{1}{2}} + 3x^{-1} + c dx$  or  $-4x^{-\frac{1}{2}} + 3x^{-1} + c = 0$  with no correct expression seen earlier are both A0. Ignore  $y = \dots$

### Alternative method: integration by parts

$$\text{e.g. } \int \frac{2\sqrt{x}-3}{x^2} dx = \int (2\sqrt{x}-3)x^{-2} dx = -(2x^{\frac{1}{2}}-3)x^{-1} + \int x^{-\frac{3}{2}} dx$$

$$-(2x^{\frac{1}{2}}-3)x^{-1} + \int x^{-\frac{3}{2}} dx = -2x^{-\frac{1}{2}} + 3x^{-1} - 2x^{-\frac{1}{2}} + c = -4x^{-\frac{1}{2}} + 3x^{-1} + c$$

M1: For attempting integration by parts and achieving the correct structure for the intermediate stage

e.g.  $\pm(\dots x^{\frac{1}{2}} \pm \dots)x^{-1} \pm \int x^{-\frac{3}{2}} dx$  or equivalent. Indices do not need to be processed

e.g.  $x^{-2} \left( \dots x^{\frac{3}{2}} \pm \dots x \right) \pm \int \dots x^{-3} \left( \dots x^{\frac{3}{2}} \pm \dots x \right) dx$

A1:  $-(2x^{\frac{1}{2}} - 3)x^{-1} + \int x^{-\frac{3}{2}} dx$  or  $x^{-2} \left( \frac{4}{3}x^{\frac{3}{2}} - 3x \right) - \int -2x^{-3} \left( \frac{4}{3}x^{\frac{3}{2}} - 3x \right) dx$  o.e.

dM1: For completing the integration by parts method achieving at least one term with a correct index (the index does not need to be processed) and terms with the same index do not need to be collected for this mark

A1: As above in the main scheme (see notes)