

Question	Scheme	Marks	AOs
<b>11(a)</b>	At $t = 0$ , $V_A = 100 + 20 = 120 \Rightarrow p = 2 \times "120"$	M1	1.1b
	$(p =) 240$	A1	1.1b
		(2)	
<b>(b)</b>	$\dots e^{0.04T} = \dots e^{-0.02T}$	M1	3.1b
	$0.8e^{0.04T} = "4.8" e^{-0.02T}$	A1ft	1.1b
	$\dots e^{0.04T} = \dots e^{-0.02T} \Rightarrow e^{\pm 0.06T} = \dots$	dM1	3.1a
	$(T =) \text{awrt } 29.9 \text{ (months)}$	A1cso	1.1b
		(4)	

**(6 marks)**

### Notes

**(a)**

M1: Attempts to find the price per gram of metal A at  $t = 0$ , and then doubles this to find the value of  $p$ . Can be implied by 240. An expression must be evaluated to score this mark

A1: 240 only (withhold this mark if they find  $V_B = 240$  but proceed to state  $p$  as a different value)

**(b)** Candidates who state that  $\frac{dV_B}{dt} = "4.8" e^{-0.02T}$  can still score full marks question (they had already determined that they needed to take the modulus of the gradient function)

May be in terms of  $t$  or  $T$

M1: Attempts to set  $\pm \frac{dV_A}{dt}$  equal to  $\pm \frac{dV_B}{dt}$ . Look for an equation of the form  $pe^{0.04T} = qe^{-0.02T}$  where  $p$  and  $q$  are constants or may be implied by further work. e.g.  $e^{\pm 0.06T} = \dots$  (it cannot be for awrt 29.9). Do not allow  $\dots Te^{0.04T} = \dots Te^{-0.02T}$

A1ft:  $0.8e^{0.04T} = "4.8" e^{-0.02T}$ . Follow through on their positive value for  $p$ .

May be implied by further work which is not awrt 29.9.

dM1: Rearranges their  $\frac{dV_A}{dt} = -\frac{dV_B}{dt}$  which cannot be the original functions to  $re^{\pm 0.06T} = s$

where  $r \times s > 0$

$\frac{dV_B}{dt} = "4.8" e^{-0.02T} \Rightarrow 0.8e^{0.04T} = "4.8" e^{-0.02T}$  is allowed (see note at the start of (b)).

Condone slips. It is dependent on the first method mark.

If they take lns of both sides first

e.g.  $0.8e^{0.04T} = "4.8" e^{-0.02T} \Rightarrow \ln 0.8 + 0.04T = \ln "4.8" - 0.02T$  they need to rearrange to  $\pm 0.06T = \dots$  by adding / subtracting.

A1cso: awrt 29.9 provided evidence of solving  $0.8e^{0.04T} = 4.8e^{-0.02T}$  is seen. i.e. they cannot proceed from  $e^{\pm 0.06T} = \dots$  to the awrt 29.9 in one step. We must see either an expression for  $t$  or e.g. taking lns of both sides.

Condone  $(T =) \frac{50 \ln 6}{3}$  or others in the form  $(T =) a \ln b$  where  $a$  and  $b$  are rational

constants e.g.  $\frac{\ln 6}{0.06}$ . It cannot be scored for an expression.