

| Question | Scheme | Marks | AOs |
|--------------|--------------------------------------------------------------------------------------------------|------------|------|
| 12(a) | $3\sin\theta\frac{\sin\theta}{\cos\theta}=4$ | M1 | 1.1b |
| | $3(1-\cos^2\theta)=4\cos\theta$ | M1 | 1.1b |
| | $3\cos^2\theta+4\cos\theta-3=0^*$ | A1* | 2.1 |
| | | (3) | |
| (b) | $3\cos^2 2x+4\cos 2x-3=0\Rightarrow\cos 2x=\frac{-4\pm\sqrt{16-4\times 3\times(-3)}}{2\times 3}$ | M1 | 1.1b |
| | $(\cos 2x)=\frac{-2+\sqrt{13}}{3}$ | A1 | 2.3 |
| | $x=\frac{\cos^{-1}\left(\frac{-2+\sqrt{13}}{3}\right)}{2}$ | dM1 | 1.1b |
| | awrt 28.8° , awrt 151.2° | A1 | 1.1b |
| | | (4) | |

(7 marks)

Notes

(a)

M1: Uses $\tan\theta=\frac{\sin\theta}{\cos\theta}$

M1: Uses $\pm\sin^2\theta\pm\cos^2=\pm 1$ to achieve an equation in terms of $\cos\theta$

A1*: Achieves the given answer $3\cos^2\theta+4\cos\theta-3=0$ with no errors seen including invisible brackets

(b)

M1: Attempts to solve $3\cos^2 2x+4\cos 2x-3=0$ by either completing the square or using the quadratic formula or using a calculator.

A1: Deduces $(\cos 2x)=\frac{-2+\sqrt{13}}{3}$ (the other root if found must be rejected / no other solutions found)

dM1: Attempts to find an angle in the given range for their solution to the quadratic using the correct processing. May be implied by awrt 29 or awrt 151.

A1: awrt 28.8° , awrt 151.2° and no others in the range. The previous three marks must have been scored (answers with no working score no marks).