

Question	Scheme	Marks	AOs
4(a)(i) (a)(ii)	$x^2 + y^2 + 10x - 4y + 1 = 0$		
	$(x+5)^2 + (y-2)^2$	M1	1.1b
	Centre $(-5, 2)$	A1	1.1b
	Radius is $\sqrt{28}$	A1	1.1b
		(3)	
(b)	$2+2\sqrt{7}$ or $2-2\sqrt{7}$ seen	B1	2.2a
	$2-2\sqrt{7} < k < 2+2\sqrt{7}$	M1	1.1b
	$\{k : 2-2\sqrt{7} < k < 2+2\sqrt{7}\}$ oe	A1	2.5
		(3)	
(6 marks)			

Notes:

Condone mislabelled parts e.g. labelled as (a), (b) and (c) not (a)(i), (a)(ii), (b)

- (a)

M1:

Attempts to complete the square by halving both x and y terms.

Award for sight of $(x \pm 5)^2 \dots (y \pm 2)^2$ or $(x \pm 5)^2$ and $(y \pm 2)^2$ seen separately.

May be implied by a centre of $(\pm 5, \pm 2)$

A1:

Correct coordinates $(-5, 2)$ or e.g. $x = -5, y = 2$ and condone e.g. $-5, 2$

A1:

$\sqrt{28}$ (or $2\sqrt{7}$)
- (b)

B1:

$2+2\sqrt{7}$ or $2-2\sqrt{7}$ seen. Accept $\sqrt{28}$ for $2\sqrt{7}$ throughout this question.

M1:

" $2-2\sqrt{7} < k < 2+2\sqrt{7}$ "

Selects the inside interval for **their** endpoints which must come from a correct method condoning slips. Condone use of y for k .

May be seen separately e.g. " $2-2\sqrt{7} < k, k < 2+2\sqrt{7}$ "

Condone e.g. " $2 - \sqrt{28} \leq k \leq 2 + \sqrt{28}$ " and allow inexact e.g. " $- 3.291 \dots < k < 7.291 \dots$ "

An incorrect method would include e.g. $5 - 2\sqrt{7} < k < 5 + 2\sqrt{7}$ ie using the x coordinate of the centre rather than the y coordinate.

A1:

Correct answer in exact form in set notation or interval notation in terms of k .

Allow: $\{k : 2-2\sqrt{7} < k < 2+2\sqrt{7}\}$ or $\{k : 2-2\sqrt{7} < k\} \cap \{k : k < 2+2\sqrt{7}\}$ or $\{2-2\sqrt{7} < k < 2+2\sqrt{7}\}$ or $\{2-2\sqrt{7} < k\} \cap \{k < 2+2\sqrt{7}\}$ or $(2-2\sqrt{7}, 2+2\sqrt{7})$ or $\{k : 2-2\sqrt{7} < k \cap k < 2+2\sqrt{7}\}$ or $\{k : 2-2\sqrt{7} < k\}$ and $\{k : k < 2+2\sqrt{7}\}$ but **not** $\{2-2\sqrt{7} < k\} \cup \{k < 2+2\sqrt{7}\}$ and **not** $[2-2\sqrt{7}, 2+2\sqrt{7}]$ and **not** $\{2-2\sqrt{7} \leq k \leq 2+2\sqrt{7}\}$

(b) Alternative 1 (substitutes $y = k$ into the given or their circle equation and uses $b^2 - 4ac = 0$ or $b^2 - 4ac > 0$)

Scores in the same way following e.g.

$$x^2 + 10x + (k^2 - 4k + 1) = 0, 10^2 - 4(k^2 - 4k + 1) > 0, 24 + 4k - k^2 = 0$$

B1: $2 + 2\sqrt{7}$ or $2 - 2\sqrt{7}$ seen. Accept $\sqrt{28}$ for $2\sqrt{7}$ throughout this question.

M1: " $2 - 2\sqrt{7} < k < 2 + 2\sqrt{7}$ "

Selects the inside interval for their endpoints which must come from a correct method condoning slips. Condone use of y for k .

May be seen separately e.g. " $2 - 2\sqrt{7} < k, k < 2 + 2\sqrt{7}$ "

Condone e.g. " $2 - \sqrt{28} \leq k \leq 2 + \sqrt{28}$ " and allow inexact

e.g. " $-3.291... < k < 7.291...$ "

If when finding their endpoints they make a sign error and obtain e.g. $k^2 - 4k - 24 > 0$ and then choose the outside region, this scores M1 but it must be consistent with their inequality.

A1: Correct answer in exact form in set notation or interval notation in terms of k .

Allow: $\{k : 2 - 2\sqrt{7} < k < 2 + 2\sqrt{7}\}$ or $\{k : 2 - 2\sqrt{7} < k\} \cap \{k : k < 2 + 2\sqrt{7}\}$ or

$\{2 - 2\sqrt{7} < k < 2 + 2\sqrt{7}\}$ or $\{2 - 2\sqrt{7} < k\} \cap \{k < 2 + 2\sqrt{7}\}$ or $(2 - 2\sqrt{7}, 2 + 2\sqrt{7})$ or

$\{k : 2 - 2\sqrt{7} < k \cap k < 2 + 2\sqrt{7}\}$ or $\{k : 2 - 2\sqrt{7} < k\}$ and $\{k : k < 2 + 2\sqrt{7}\}$ but **not**

$\{2 - 2\sqrt{7} < k\} \cup \{k < 2 + 2\sqrt{7}\}$ and **not** $[2 - 2\sqrt{7}, 2 + 2\sqrt{7}]$ and **not**

$\{2 - 2\sqrt{7} \leq k \leq 2 + 2\sqrt{7}\}$

(b) Alternative 2 (substitutes $x = -5$ into the given or their circle equation and solves for y)
Scores in the same way following e.g.

$$25 + y^2 - 50 - 4y + 1 - 0 \Rightarrow y^2 - 4y - 24 = 0 \Rightarrow y =$$

B1: $2 + 2\sqrt{7}$ or $2 - 2\sqrt{7}$ seen. Accept $\sqrt{28}$ for $2\sqrt{7}$ throughout this question.

M1: " $2 - 2\sqrt{7} < k < 2 + 2\sqrt{7}$ "

Selects the inside interval for their endpoints which must come from a correct method condoning slips. Condone use of y for k .

May be seen separately e.g. " $2 - 2\sqrt{7} < k, k < 2 + 2\sqrt{7}$ "

Condone e.g. " $2 - \sqrt{28} \leq k \leq 2 + \sqrt{28}$ " and allow inexact

e.g. " $-3.291... < k < 7.291...$ "

A1: Correct answer in exact form in set notation or interval notation in terms of k .

Allow: $\{k : 2 - 2\sqrt{7} < k < 2 + 2\sqrt{7}\}$ or $\{k : 2 - 2\sqrt{7} < k\} \cap \{k : k < 2 + 2\sqrt{7}\}$ or

$\{2 - 2\sqrt{7} < k < 2 + 2\sqrt{7}\}$ or $\{2 - 2\sqrt{7} < k\} \cap \{k < 2 + 2\sqrt{7}\}$ or $(2 - 2\sqrt{7}, 2 + 2\sqrt{7})$ or

$\{k : 2 - 2\sqrt{7} < k \cap k < 2 + 2\sqrt{7}\}$ or $\{k : 2 - 2\sqrt{7} < k\}$ and $\{k : k < 2 + 2\sqrt{7}\}$ but **not**

$\{2 - 2\sqrt{7} < k\} \cup \{k < 2 + 2\sqrt{7}\}$ and **not** $[2 - 2\sqrt{7}, 2 + 2\sqrt{7}]$ and **not**

$\{2 - 2\sqrt{7} \leq k \leq 2 + 2\sqrt{7}\}$