

Question Number	Scheme	Marks	AOs
5 (a)	Attempts correct cosine rule $\cos \theta^\circ = \frac{4^2 + 5^2 - 7^2}{2 \times 4 \times 5}$	M1	1.1b
	$\cos \theta^\circ = \left\{ \frac{-8}{40} \right\} - \frac{1}{5} *$	A1*	1.1b
		(2)	
(b)	Uses e.g. $\sin^2 \theta + \cos^2 \theta = 1 \Rightarrow \sin^2 \theta + \frac{1}{25} = 1 \Rightarrow \sin^2 \theta = \dots$	M1	3.1a
	$\sin \theta^\circ = \sqrt{\frac{24}{25}} = \left(\frac{2\sqrt{6}}{5} \right)$	A1	1.1b
	Attempts to find the area $= \frac{1}{2} \times 4 \times 5 \times \sqrt{\frac{24}{25}}$	M1	2.1
	$= 4\sqrt{6} \text{ (cm}^2\text{)}$	A1	1.1b
		(4)	
(6 marks)			
Notes:			

(a)

M1: Attempts the cosine rule the correct way round $\cos \theta^\circ = \frac{4^2 + 5^2 - 7^2}{2 \times 4 \times 5}$ o.e. such as

$$7^2 = 4^2 + 5^2 - 2 \times 4 \times 5 \cos \theta^\circ$$

The formula they are substituting into should be correct, with values in the correct place, but condone e.g. a sign slip when they substitute provided a correct formula has been seen.

Allow any argument to be used (that is not clearly incorrect e.g. C).

A1*: Arrives at the given answer through correct work and no errors.

There is no need to see the degrees symbol at any point. Should be using θ but condone A or BAC in the final line. It is acceptable for other arguments to be used in their previous work but recovered in their final line to either θ , A or BAC provided they are not clearly incorrect e.g. C

Condone e.g. -0.2 or $\frac{-1}{5}$ or $\frac{1}{-5}$ for $-\frac{1}{5}$ and there is no need to see $-\frac{8}{40}$

(b)

M1: Uses $\pm \sin^2 \theta \pm \cos^2 \theta = \pm 1$ o.e. and proceeds to find an exact value for $\sin \theta$ or $\sin^2 \theta$ which may be implied by later work.

Alternatively, uses a right-angled triangle with sides ± 1 , ± 5 and $\pm \sqrt{24}$ in the correct places to find an exact value for $\sin \theta$ or $\sin^2 \theta$. May be implied (and you may not see the triangle).

Not scored for use of $\sin \left(\cos^{-1} \left(-\frac{1}{5} \right) \right)$

You may see attempts splitting triangle ABC into two right-angled triangles and then use of Pythagoras to find the height and lengths of these right-angled triangles. See the alternate mark scheme at the end or use review if unsure.

A1: Correct exact value for $\sin \theta$ which may be unsimplified. Condone inclusion of $\pm$

$\sin \theta = \sqrt{\frac{24}{25}} \left(\text{or } \frac{2\sqrt{6}}{5} \right)$ following sight of 101.5... and without a method seen does **not** imply

M1A1. However, $\sin \theta = \sqrt{\frac{24}{25}} \left(\text{or } \frac{2\sqrt{6}}{5} \right)$ without sight of 101.5... implies M1A1.

M1: Complete method to find the area of the triangle, which may be inexact.

While this mark is not dependent on the previous method mark, it does require a correct method to find a value for $\sin \theta$ or $\sin^2 \theta$.

Note that they may use the sine rule to find one of the other angles and then attempt

e.g. $\frac{1}{2} \times 7 \times 4 \times \sin ABC$

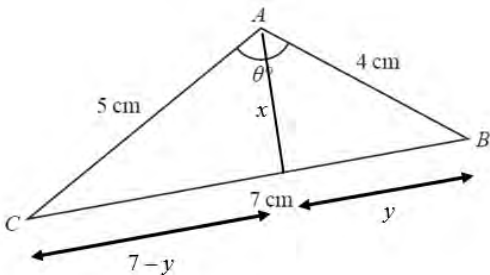
Condone, for this mark only, attempts that use $\sin \left(\cos^{-1} \left(-\frac{1}{5} \right) \right)$ or e.g. $\sin(101.5\dots)$

A1: $4\sqrt{6} \text{ cm}^2$ must be simplified and must follow award of the previous 3 marks.

Note that some are using $\theta = 101.5\dots$, finding area = awrt 9.80 and then realising this is $4\sqrt{6}$ (or $\sqrt{96}$) and score only the second M mark without an otherwise correct method.

Ignore incorrect units.

Alt (b): Splitting triangle ABC and using Pythagoras (condoned)



M1: Complete method to split triangle ABC into two right-angled triangles and use Pythagoras and simultaneous equations to find the perpendicular height of the two right-angled triangles. e.g.

$(7-y)^2 + x^2 = 5^2$ and $y^2 + x^2 = 4^2 \Rightarrow 49 - 14y = 25 - 16 \Rightarrow y = \dots \left\{ \frac{20}{7} \right\} \Rightarrow x = \dots \left\{ \frac{8\sqrt{6}}{7} \right\}$

A1: Correct exact perpendicular height of the right-angled triangles.

Note the perpendicular height to BC is $\frac{8\sqrt{6}}{7}$, to AC is $\frac{8\sqrt{6}}{5}$ and to AB is $2\sqrt{6}$

M1: Complete method to find the area of triangle ABC, which may be inexact.

e.g. $\frac{1}{2} \times 7 \times \frac{8\sqrt{6}}{7}$ or $\frac{1}{2} \times 5 \times \frac{8\sqrt{6}}{5}$ or $\frac{1}{2} \times 4 \times 2\sqrt{6}$

or even e.g. $\frac{1}{2} \times \frac{20}{7} \times \frac{8\sqrt{6}}{7} + \frac{1}{2} \times \left(7 - \frac{20}{7} \right) \times \frac{8\sqrt{6}}{7}$

While this mark is not dependent on the previous method mark, it does require a correct method to find a value for the perpendicular height of the triangle.

A1: As main scheme.