

Question Number	Scheme	Marks	AOs
6 (a)	Attempts a scale factor $\frac{10}{4}, \frac{4}{10}$ o.e.	M1	3.1a
	$p = -15$	A1	1.1b
		(2)	
(b)	Attempts either $ \mathbf{a} + \mathbf{c} = \left \begin{pmatrix} 4+q \\ -3 \end{pmatrix} \right = \sqrt{(4+q)^2 + 9}$ or $ \mathbf{d} = \sqrt{30^2 + 6^2} \quad \{ = \sqrt{936} = 6\sqrt{26} \}$	M1	1.1b
	$2 \mathbf{a} + \mathbf{c} = \mathbf{d} \Rightarrow 4((4+q)^2 + 9) = 30^2 + 6^2 \quad \{ = 936 \}$	dM1	1.1b
	$(4+q)^2 = 225 \Rightarrow 4+q = \pm 15 \Rightarrow q = \dots$ or $q^2 + 8q - 209 = 0 \Rightarrow q = \dots$	ddM1	2.1
	$\Rightarrow q = 11, -19$	A1	1.1b
		(4)	
(6 marks)			
Notes:			

- (a)
- M1: Uses the fact that the vectors are parallel and attempts a scale factor.
May be implied by e.g. $\begin{pmatrix} 4 \\ -6 \end{pmatrix} = \lambda \begin{pmatrix} 10 \\ p \end{pmatrix} \Rightarrow \lambda = \dots$ or $4 = 10\lambda \Rightarrow \lambda = \dots$
- A1: $p = -15$ Sight of this with no incorrect working scores both marks including e.g. $\begin{pmatrix} 10 \\ -15 \end{pmatrix}$
Note $p = -15\mathbf{j}$ scores M1A0.
- (b)
- M1: Attempts a correct method of finding the modulus or modulus² for either vector $\mathbf{a} + \mathbf{c}$ or $\mathbf{d}$.
If using $\mathbf{a} + \mathbf{c}$ then they must clearly be adding the vectors.
Condone incorrect labelling, e.g., $|\mathbf{a} + \mathbf{c}| = (4+q)^2 + 9$ as it is not a “show that”.
- dM1: Uses the information to set up a quadratic equation in q with square roots removed.
Dependent on the previous method mark.
When finding $|\mathbf{a} + \mathbf{c}|$ they must clearly be adding the vectors.

Correct algebraic work is required but condone poor squaring e.g. $(4+q)^2 = 16 + q^2$ and numerical slips such as failure to square the 2 i.e. $2((4+q)^2 + 9) = 30^2 + 6^2$ or omission of the
i.e. $(4+q)^2 + 9 = 30^2 + 6^2$
Similarly, condone failure to multiply both components of $\mathbf{a} + \mathbf{c}$ by 2 leading to e.g.
 $\sqrt{(8+2q)^2 + 3^2} = \sqrt{30^2 + 6^2}$

Use of $|\mathbf{a} + \mathbf{c}| \rightarrow |\mathbf{a}| + |\mathbf{c}|$ is dM0, as is poor square rooting e.g. $\sqrt{q^2 + 8q + 25} = \sqrt{q^2 + 8q} + 5$

ddM1: Full and complete attempt to find at least one value for q , condoning failure to square the 2 or similar.

Dependent on both previous method marks.

If they expand the brackets, then for this mark they must achieve a 3TQ and go on to solve it using the usual rules. They may also use a calculator, in which case values will need checking.

Note that the correct 3TQ is $4q^2 + 32q - 836 = 0$ or $q^2 + 8q - 209 = 0$

Note also that if they fail to square the 2 then they are likely to achieve $2q^2 + 16q - 886 = 0$ or $q^2 + 8q - 443 = 0$ which leads to $q = -4 \pm 3\sqrt{51}$

A1: cao Both $q = 11, -19$ and no others. Must be simplified. A0 if either value is rejected.

Note: You may see correct answers coming from incorrect work,

$$\text{e.g. } 4((4+q)^2 - 9) = 30^2 - 6^2 \text{ which will score M0dM0ddM0A0}$$

Alt(b): You may see perfectly valid responses such as

$$2 \begin{vmatrix} 4+q \\ -3 \end{vmatrix} = \begin{vmatrix} 30 \\ 6 \end{vmatrix} \Rightarrow \begin{vmatrix} 8+2q \\ -6 \end{vmatrix} = \begin{vmatrix} 30 \\ 6 \end{vmatrix} \Rightarrow \pm(8+2q) = 30 \Rightarrow q = 11, -19$$

M1: Sets up the modulus equation $\begin{vmatrix} 8+2q \\ -6 \end{vmatrix} = \begin{vmatrix} 30 \\ 6 \end{vmatrix}$ which may be implied by either $|8+2q| = 30$

or **both** $8+2q = 30$ **and** $-8-2q = 30$

Condone a slip on the **i** component e.g. $\begin{vmatrix} 8+q \\ -6 \end{vmatrix} = \begin{vmatrix} 30 \\ 6 \end{vmatrix}$

dM1: Deduces **either** linear equation in q following the award of the previous mark.

ddM1: For solving **both** linear equations in q

A1: cao Both $q = 11, -19$ and no others. Must be simplified. A0 if either value is rejected.