

Qu	Scheme						Marks	AOs														
4(a)	Let A = the number of green beads in a pack $A \sim B(10, 0.38)$ $\left[P(A > 6) = 1 - P(A \leq 6) \right]$						M1	3.4														
	$= 1 - 0.9586... = \text{awrt } 0.0413$						A1	1.1b														
							(2)															
(b)	<table><tr><td>a</td><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td></tr><tr><td>$P(A = a)$</td><td>8.392×10^{-3}</td><td>0.0514...</td><td>0.1418...</td><td>0.2318...</td><td>0.2487...</td><td>0.1829...</td></tr></table>	a	0	1	2	3	4	5	$P(A = a)$	8.392×10^{-3}	0.0514...	0.1418...	0.2318...	0.2487...	0.1829...						M1	1.1b
	a	0	1	2	3	4	5															
	$P(A = a)$	8.392×10^{-3}	0.0514...	0.1418...	0.2318...	0.2487...	0.1829...															
	<table><tr><td>a</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr><tr><td>$P(A = a)$</td><td>0.0934...</td><td>0.0327...</td><td>7.52×10^{-3}</td><td>1.024×10^{-3}</td><td>6.278×10^{-5}</td></tr></table>	a	6	7	8	9	10	$P(A = a)$	0.0934...	0.0327...	7.52×10^{-3}	1.024×10^{-3}	6.278×10^{-5}									
	a	6	7	8	9	10																
$P(A = a)$	0.0934...	0.0327...	7.52×10^{-3}	1.024×10^{-3}	6.278×10^{-5}																	
Most likely number of green beads is 4 together with $P(A = 3) = 0.2318..., P(A = 4) = 0.2487..., P(A = 5) = 0.1829...$						A1	2.4															
						(2)																
(c)	$H_0 : p = 0.2 \quad H_1 : p > 0.2$						B1	2.5														
	Let F = number of faulty bowls $F \sim B(40, 0.2)$ <u>or</u> $P(F \leq 12) = 0.9568... > 0.95$ or $P(F \geq 13) = \text{awrt } 0.043... [< 0.05]$						M1	3.3														
	CR: $\{ F \geq 13 \}$						A1	1.1b														
							(3)															
(d)	awrt 0.043						B1ft	1.1b														
							(1)															
(e)	17 is in the CR, sufficient evidence to <u>support</u> the manager's <u>belief</u> or <u>proportion</u> of faulty bowls is <u>less than</u> 20%						B1ft	2.2b														
							(1)															
(f)	A valid model because e.g. <u>random</u> sampling guarantees <u>independence</u> or <u>constant probability</u>						B1	3.5a														
							(1)															

(10 marks)

Notes:

- (a) M1:** for selecting and using a suitable model, sight of $B(10, 0.38)$ o.e. in words
Can be implied by $P(A \leq 6) = \text{awrt } 0.959$ or final answer = awrt 0.0413
A1: for awrt 0.0413
- (b) M1:** for finding the probability of at least 2 different numbers of green beads or $\frac{0.38}{r+1} > \frac{0.62}{10-r}$ o.e.
A1: for 4 & $P(A = 3) = 0.2318..., P(A = 4) = 0.2487..., P(A = 5) = 0.1829..$ (accept 2dp) or $r < 3.18$
- (c) B1:** for correctly stating both hypotheses in terms of p or π
M1: For use of tables of $B(40, 0.2)$ to find probability associated with critical value
 $[P(F \leq 12) = \text{awrt } 0.957$ or $P(F \geq 13) = \text{awrt } 0.043$ (may be implied by either correct probability or by the correct CR)]
A1: $[40 \geq] F \geq 13$ o.e. e.g. $F > 12$ Allow '13 or more' or 'CR ≥ 13 ' Correct ans only M1A1
- (d) B1ft:** awrt 0.043 (allow awrt 4.3%) or correct ft their one-tailed upper CR from $B(40, 0.2)$ to 3s.f.

<p>(e) B1ft: For commenting on the manager's belief, ft their (c)</p>
<p>(f) B1: Binomial is a valid model with a suitable reason. Must see underlined words.</p>