

4.

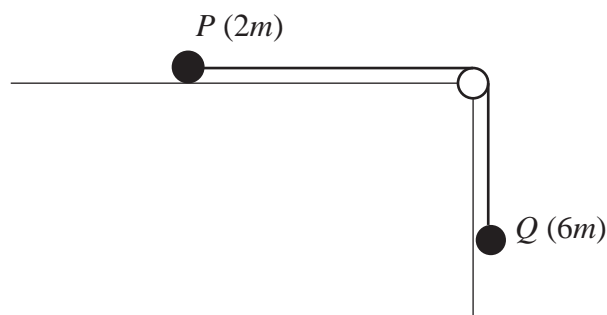


Figure 1

Two balls,  $P$  and  $Q$ , have masses  $2m$  and  $6m$  respectively.

The balls are attached to the ends of a rope that passes over a pulley. The pulley is fixed at the edge of a horizontal table.

Ball  $P$  is held at rest on the table, with the rope taut and  $Q$  hanging vertically below the pulley, as shown in Figure 1.

The system is released from rest and the balls move.

In a model of the motion

- the balls are modelled as particles
- the rope is modelled as being light and inextensible
- the pulley is modelled as being small and smooth
- air resistance is modelled as being negligible

In the motion

- $Q$  moves downwards with an acceleration of magnitude  $\frac{7g}{16}$
- the total resistance to the motion of  $P$  has magnitude  $kmg$ , where  $k$  is a constant
- the tension in the rope either side of the pulley is  $T$

Using the model,

- (a) write down an equation of motion for  $P$ , giving your answer in terms of  $T$ ,  $k$ ,  $m$  and  $g$ ,

(2)

- (b) find the value of  $k$ .

(4)

In reality, the pulley would **not** be smooth.

- (c) State how this would affect the tension in the rope.

(1)

The model is refined so that the pulley is modelled as **not** being smooth.

- (d) Suggest **one** further refinement of the model, apart from including air resistance, that would make the model more realistic.

(1)