

Question	Scheme	Marks	AOs
4	$4 + \cos 2\theta = \frac{9}{2} \Rightarrow \theta = \dots$	M1	3.1a
	$\theta = \frac{\pi}{6}$	A1	1.1b
	$\frac{1}{2} \int (4 + \cos 2\theta)^2 d\theta = \frac{1}{2} \int (16 + 8\cos 2\theta + \cos^2 2\theta) d\theta$	M1	3.1a
	$\cos^2 2\theta = \frac{1}{2} + \frac{1}{2} \cos 4\theta \Rightarrow A = \frac{1}{2} \int \left( 16 + 8\cos 2\theta + \frac{1}{2} + \frac{1}{2} \cos 4\theta \right) d\theta$	M1	3.1a
	$= \frac{1}{2} \left[ 16\theta + 4\sin 2\theta + \frac{\sin 4\theta}{8} + \frac{\theta}{2} \right]$	A1	1.1b
	Using limits 0 and their $\frac{\pi}{6}$ : $\frac{1}{2} \left[ \frac{33\pi}{12} + 2\sqrt{3} + \frac{\sqrt{3}}{16} - (0) \right]$	M1	1.1b
	Area of triangle = $\frac{1}{2}(r \cos \theta)(r \sin \theta) = \frac{1}{2} \times \frac{81}{4} \times \frac{1}{2} \times \frac{\sqrt{3}}{2}$	M1	3.1a
	Area of R = $\frac{33\pi}{24} + \frac{33\sqrt{3}}{32} - \frac{81\sqrt{3}}{32}$	M1	1.1b
	$= \frac{11}{8}\pi - \frac{3\sqrt{3}}{2} \left( p = \frac{11}{8}, q = -\frac{3}{2} \right)$	A1	1.1b

(9 marks)

**Notes:****M1:** Realises the angle for  $A$  is required and attempts to find it**A1:** Correct angle**M1:** Uses a correct area formula and squares  $r$  to achieve a 3TQ integrand in  $\cos 2\theta$ **M1:** Use of the correct double angle identity on the integrand to achieve a suitable form for integration**A1:** Correct integration**M1:** Correct use of limits**M1:** Identifies the need to subtract the area of a triangle and so finds the area of the triangle**M1:** Complete method for the area of  $R$ **A1:** Correct final answer