

Question	Scheme	Marks	AOs
6(a)	$f(x) = \frac{x+2}{x^2+9} = \frac{x}{x^2+9} + \frac{2}{x^2+9}$	B1	3.1a
	$\int \frac{x}{x^2+9} dx = k \ln(x^2+9)(+c)$	M1	1.1b
	$\int \frac{2}{x^2+9} dx = k \arctan\left(\frac{x}{3}\right)(+c)$	M1	1.1b
	$\int \frac{x+2}{x^2+9} dx = \frac{1}{2} \ln(x^2+9) + \frac{2}{3} \arctan\left(\frac{x}{3}\right) + c$	A1	1.1b
		(4)	
(b)	$\int_0^3 f(x) dx = \left[\frac{1}{2} \ln(x^2+9) + \frac{2}{3} \arctan\left(\frac{x}{3}\right) \right]_0^3$ $= \frac{1}{2} \ln 18 + \frac{2}{3} \arctan\left(\frac{3}{3}\right) - \left(\frac{1}{2} \ln 9 + \frac{2}{3} \arctan(0) \right)$ $= \frac{1}{2} \ln \frac{18}{9} + \frac{2}{3} \arctan\left(\frac{3}{3}\right)$	M1	1.1b
	Mean value = $\frac{1}{3-0} \left(\frac{1}{2} \ln 2 + \frac{\pi}{6} \right)$	M1	2.1
	$\frac{1}{6} \ln 2 + \frac{1}{18} \pi^*$	A1*	2.2a
		(3)	
(c)	$\frac{1}{6} \ln 2 + \frac{1}{18} \pi + \ln k$	M1	2.2a
	$\frac{1}{6} \ln 2k^6 + \frac{1}{18} \pi$	A1	1.1b
		(2)	

(9 marks)

Notes:

(a)

B1: Splits the fraction into two correct separate expressions

M1: Recognises the required form for the first integration

M1: Recognises the required form for the second integration

A1: Both expressions integrated correctly and added together with constant of integration included

(b)

M1: Uses limits correctly and combines logarithmic terms

M1: Correctly applies the method for the mean value for their integration

A1*: Correct work leading to the given answer

(c)

M1: Realises that the effect of the transformation is to increase the mean value by $\ln k$

A1: Combines \ln 's correctly to obtain the correct expression