

| Question | Scheme   | Marks | AOs  |
|----------|--|-------|------|
| 1        | 6(1 + 2sinh <sup>2</sup> x) + 4sinh x = 7 and rearranges to quadratic form<br>OR substitutes correct exponential identities and rearranges to quartic in e <sup>x</sup> , cosh 2x = $\frac{e^{2x} + e^{-2x}}{2}$ and sinh x = $\frac{e^x - e^{-x}}{2}$ used. | M1    | 3.1a |
|          | 12sinh <sup>2</sup> x + 4sinh x - 1 = 0 OR 3e <sup>4x</sup> + 2e <sup>3x</sup> - 7e <sup>2x</sup> - 2e <sup>x</sup> + 3 = 0  | A1    | 1.1b |
|          | (6sinh x - 1)(2sinh x + 1) = 0 ⇒ sinh x = ...<br>OR (e <sup>2x</sup> + e <sup>x</sup> - 1)(3e <sup>2x</sup> - e <sup>x</sup> - 3) = 0 ⇒ e <sup>x</sup> = ....  | M1    | 1.1b |
|          | sinh x = $\frac{1}{6}$ or sinh x = $-\frac{1}{2}$<br>OR e <sup>x</sup> = $\frac{-1 \pm \sqrt{5}}{2}$ or e <sup>x</sup> = $\frac{1 \pm \sqrt{37}}{6}$   | A1    | 1.1b |
|          | x = ln(a + √(1 + a <sup>2</sup> )) where a is one of their sinh x values<br>OR undoes exponentials using ln  | M1    | 1.2  |
|          | x = ln( $\frac{1 + \sqrt{37}}{6}$ ), x = ln( $\frac{-1 + \sqrt{5}}{2}$ )   | A1    | 1.1b |
|          |  | (6)   |      |

(6 marks)

**Notes:**

**M1:** Identifies a correct approach to solving the problem, either through use of identity or definition of hyperbolics

**A1:** Reaches a correct quadratic in sinh x or a correct quartic in e<sup>x</sup>.

**M1:** Solves their quadratic/quartic, may just see answers from calculator.

**A1:** Correct values for sinh x or e<sup>x</sup> found.

**M1:** Correct process of reaching x from their solutions in sinh x or e<sup>x</sup>

**A1:** Correct answers as exact simplified logarithms, and no others (in the alternative the negative exponential cases must have been rejected).