**2.**

$$zz^* + 3\mathrm{i}z = p + 9\mathrm{i}$$

where $z$ is a complex number and $p$ is a real constant.

Given that this equation has exactly one root, determine the complex number $z$.

**(5)**