

Question	Scheme	Marks	AOs
3	$w = 4x - 1 \Rightarrow x = \frac{w+1}{4}$	B1	3.1a
	$a\left(\frac{w+1}{4}\right)^3 + b\left(\frac{w+1}{4}\right)^2 - 19\left(\frac{w+1}{4}\right) - b (= 0)$ or $(4x-1)^3 - 9(4x-1)^2 - 97(4x-1) + c (= 0)$	M1	3.1a
	$aw^3 + (3a+4b)w^2 + (3a+8b-304)w + (a-60b-304) = 0$ or $64x^3 - 192x^2 - 304x + 87 + c = 0$	M1	1.1b
	Divides by a and equates the coefficients of w^2 and w $\frac{3a+4b}{a} = -9$ $\frac{3a+8b-304}{a} = -97$ and solves simultaneously to find a value for a or a value for b Note: $12a+4b=0$ and $100a+8b=304$ or Divides through by '16' leading to values of a and b $4x^3 - 12x^2 - 19x + \frac{87+c}{19} = 0$	M1	3.1a
	$c = \frac{a-60b-304}{a} = \dots$ or $\frac{87+c}{19} = 12$ P $c = \dots$	M1	1.1b
	$a = 4$ $b = -12$ $c = 105$	A1	1.1b
		(6)	

(6 marks)

Notes:

B1: Selects the method of making a connection between x and w by writing $w = 4x - 1$ or $x = \frac{w+1}{4}$

M1: Applies the process of substituting their $x = \frac{w+1}{4}$ into $ax^3 + bx^2 - 19x - b = 0$ or $w = 4x - 1$

into $w^3 - 9w^2 - 97w + c = 0$. Must be substitution of the correct variable into the opposing equation but may be scored if the initial linear equation is incorrect (e.g. $x = 4w - 1$ into the first equation). Note that the " $= 0$ " can be missing for this mark.

M1: Expands the brackets and collects terms in their equation (in x or w). Note that the " $= 0$ " can be missing for this mark.

M1: A complete method for finding a value for a or b . See scheme, it involves dividing through by an appropriate factor for their equation to balance the w^3 or $-19x$ terms, then equating other coefficients and solving equations if necessary.

M1: A complete method for finding a value for c . They must have divided through by an appropriate factor as per the previous M before attempting to compare the constant coefficient (and use their a and b if appropriate).

A1: $a = 4$ $b = -12$ $c = 105$

Alternative			
At least two of	$\alpha + \beta + \gamma = -\frac{b}{a}$ $\alpha\beta + \alpha\gamma + \beta\gamma = -\frac{19}{a}$ $\alpha\beta\gamma = \frac{b}{a}$	B1	3.1a
New sum =	$4(\alpha + \beta + \gamma) - 3 = 9 \Rightarrow 4\left(-\frac{b}{a}\right) - 3 = 9 \Rightarrow b = -3a$	M1	3.1a
New pair sum =	$16(\alpha\beta + \alpha\gamma + \beta\gamma) - 8(\alpha + \beta + \gamma) + 3 = -97$ $\Rightarrow 16\left(-\frac{19}{a}\right) - 8\left(-\frac{b}{a}\right) + 3 = -97$	M1	1.1b
	$\Rightarrow 16\left(-\frac{19}{a}\right) - 8(3) + 3 = -97 \Rightarrow a = \dots$	M1	3.1a
New product	$64(\alpha\beta\gamma) - 16(\alpha\beta + \alpha\gamma + \beta\gamma) + 4(\alpha + \beta + \gamma) - 1 = -c$ $\Rightarrow 64\left(\frac{b}{a}\right) - 16\left(-\frac{19}{a}\right) + 4(3) - 1 = -c \Rightarrow c = \dots$	M1	1.1b
	$a = 4 \quad b = -12 \quad c = 105$	A1	1.1b
		(6)	

Alternative Notes

B1: Selects the method of giving at least two correct equations containing α , β and γ

M1: Applies the process of finding the new sum to generate an equation in a and b . Must be substituting in the correct places.

M1: Attempts the new pair sum to generate another equation connecting a and b . Must be substituting in the correct places.

M1: Solves their equations to find a value for a or b .

M1: Uses the new product with their values to find values for a , b and c

A1: $a = 4 \quad b = -12 \quad c = 105$