

Question	Scheme	Marks	AOs
<b>1(a)</b>	$f(x) = e^{2x} \cos x \Rightarrow f'(x) = 2e^{2x} \cos x - e^{2x} \sin x$	M1	1.1a
	$f''(x) = 4e^{2x} \cos x - 2e^{2x} \sin x - (2e^{2x} \sin x + e^{2x} \cos x)$	M1 A1	1.1b 1.1b
	$f''(x) = 3e^{2x} \cos x - 4e^{2x} \sin x = pe^{2x} \cos x + q(2e^{2x} \cos x - e^{2x} \sin x)$ $\Rightarrow p = \dots, q = \dots$	M1	3.1a
	$f''(x) = -5f(x) + 4f'(x)$	A1	2.1
		<b>(5)</b>	
<b>(b)</b>	$f(0) = 1, f'(0) = 2, f''(0) = 3, f'''(0) = 2, f''''(0) = -7, f^v(0) = -38$	M1	1.1b
	$f(x) = f(0) + xf'(0) + \frac{x^2}{2!} f''(0) + \dots$	M1	1.1b
	$f(x) \approx 1 + 2x + \frac{3x^2}{2} + \frac{x^3}{3} - \frac{7x^4}{24} - \frac{19x^5}{60}$	A1	2.2a
		<b>(3)</b>	

**(8 marks)**

### Notes

(a)

M1: Realises the need to use the product rule and attempts the first derivative

M1: Applies the product rule again to find the second derivative

A1: Correct second derivative simplified or un-simplified

M1: Uses their derivatives in order to obtain values for  $p$  and  $q$

A1: Completes the proof and obtains the correct values of  $p$  and  $q$

(b)

M1: Attempts all 5 derivatives at  $x = 0$  using the result from part (a)

M1: Uses the correct Maclaurin series including the factorials

A1: Correct expression