| Question | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: |
| 6 | When $n=1,3^{n}-2^{n}=1$ <br> When $n=2,3^{n}-2^{n}=9-4=5$ <br> So the result is true for $n=1$ and $n=2$ | B1 | 2.2a |
|  | Assume true for $n=k$ and $n=k+1$ so $u_{k}=3^{k}-2^{k}$ and $u_{k+1}=3^{k+1}-2^{k+1}$ | M1 | 2.4 |
|  | $u_{k+2}=5\left(3^{k+1}-2^{k+1}\right)-6\left(3^{k}-2^{k}\right)$ | M1 | 1.1b |
|  | $u_{k+2}=5 \times 3^{k+1}-5 \times 2^{k+1}-2 \times 3^{k+1}+3 \times 2^{k+1}$ | A1 | 1.1b |
|  | $\begin{gathered} =3 \times 3^{k+1}-2 \times 2^{k+1} \\ =3^{k+2}-2^{k+2} \end{gathered}$ | A1 | 2.1 |
|  | If the statement is true for $n=k$ and $n=k+1$ then it has been shown true for $n=k+2$ and as it is true for $n=1$ and $n=2$, the statement is true for all positive integers $n$. | A1 | 2.4 |
|  |  | (6) |  |

(6 marks)

## Notes

B1: Shows the statement is true for $n=1$ and $n=2$
M1: Makes a statement that assumes the result is true for $n=k$ and $n=k+1$
M1: Substitutes the assumption statements into the given result
A1: Correct expression that has been processed correctly to be in terms of $3^{k+1}$ and $2^{k+1}$
A1: Obtains $3^{k+2}-2^{k+2}$ with no errors and all working shown
A1: Correct complete conclusion that may be part of a narrative throughout the proof

