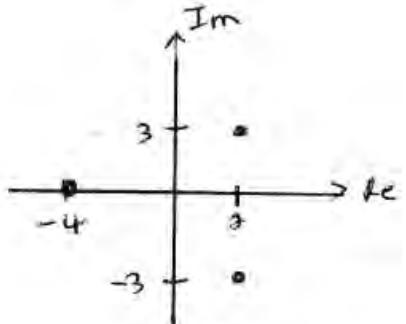


Question	Scheme	Marks	AOs
<b>1(a)</b>	$2 + 3i$	B1	1.1b
		(1)	
<b>(b) (i)</b>	$z^* = 2 + 3i$ so $z + z^* = 4, zz^* = 13$ $z + z^* + \alpha = 0 \Rightarrow \alpha = \dots$ or $\alpha zz^* = -52 \Rightarrow \alpha = -\frac{52}{13} = \dots$ or $z^2 - (\text{sum roots})z + (\text{product roots}) = 0$ or $(z - (2 + 3i))(z - (2 - 3i)) = \dots$ $\Rightarrow (z^2 - 4z + 13)(z + 4) \Rightarrow z = \dots$	M1	3.1a
	$z = 2 \pm 3i, -4$	A1	1.1b
	<b>(ii)</b> $(z^2 - 4z + 13)(z + 4)$ expands the brackets to find value for $a$ Or $a = \text{pair sum} = -4(2 + 3i + 2 - 3i) + 13 = \dots$ Or $f(-4)/f(2 \pm 3i) = 0 \Rightarrow \dots \Rightarrow a = \dots$	M1	1.1b
	$a = -3$	A1	2.2a
		(4)	
<b>(c)</b>		B1ft	1.1b
		(1)	

**(6 marks)**

**Notes:****(a)****B1:**  $2 + 3i$ **(b)****(i)**

**M1:** A complete method to find the third root. E.g. forms the quadratic factor and uses this to find the linear factor leading to roots. Alternatively uses sum of roots = 0 or product of roots =  $\pm 52$  (condone sign error) with their complex roots to find the third. Note they may have used the factor theorem to find  $a$  first, which is fine. If they have found  $a$  first, then the correct third root seen implies this mark. The method may be implied by the third root seen on the diagram.

**A1:** Correct roots, all three must be clearly stated somewhere in (b), not just seen on a diagram in part (c).

**(ii)**

**M1:** Complete method to find a value for  $a$  e.g. multiplies out their quadratic and linear factors to find the coefficient of  $z$ , or uses pair sum, or uses factor theorem with one of the roots (may be done before finding the third root) but must reach a value for  $a$ .

**A1:** Deduces the correct value of  $a$ . May be seen as the  $z$  coefficient in the cubic (need not be extracted, but if it is it must be correct).

**(c)**

**B1ft:** Correctly plots all three roots following through their third root in part (b). Must be labelled with the “ $-4$ ” further from  $O$  than 2, but don’t be concerned about  $x$  and  $y$  scale. If correct look for one root on the negative real axis, with the other two symmetric about real axis in quadrants 1 and 4, but follow through their real root if positive. Accept  $(0, -4)$  labelled on the real axis in correct place as a label.