

Question	Scheme	Marks	AOs
6(a)	$\frac{2x^2 + 3x + 6}{(x + 1)(x^2 + 4)} = \frac{A}{x + 1} + \frac{Bx + C}{x^2 + 4} \Rightarrow 2x^2 + 3x + 6 = A(x^2 + 4) + (Bx + C)(x + 1)$	M1	1.1b
	<p>e.g. $x = -1 \Rightarrow A = \dots$, $x = 0 \Rightarrow C = \dots$, coeff $x^2 \Rightarrow B = \dots$</p> <p>or</p> <p>Compares coefficients and solves to find values for A, B and C</p> $2 = A + B, \quad 3 = B + C, \quad 6 = 4A + C$	dM1	1.1b
	$A = 1, \quad B = 1, \quad C = 2$	A1	1.1b
		(3)	
(b)	$\int_0^2 \frac{1}{x+1} + \frac{x+2}{x^2+4} dx = \int_0^2 \frac{1}{x+1} + \frac{x}{x^2+4} + \frac{2}{x^2+4} dx$ $= \left[\alpha \ln(x+1) + \beta \ln(x^2+4) + \lambda \arctan\left(\frac{x}{2}\right) \right]_0^2$	M1	3.1a
	$= \left[\ln(x+1) + \frac{1}{2} \ln(x^2+4) + \arctan\left(\frac{x}{2}\right) \right]_0^2$	A1	2.1
	$= \left[\ln(3) + \frac{1}{2} \ln(8) + \arctan 1 \right] - \left[\ln(1) + \frac{1}{2} \ln(4) + \arctan(0) \right]$ $= \left[\ln(3) + \frac{1}{2} \ln(8) + \arctan(1) \right] - \left[\frac{1}{2} \ln 4 \right] = \ln\left(\frac{3\sqrt{8}}{2}\right) + \frac{\pi}{4}$	dM1	2.1
	$\ln(3\sqrt{2}) + \frac{\pi}{4}$	A1	2.2a
		(4)	
	(7 marks)		

Notes:

(a)

M1: Selects the correct form for partial fractions and multiplies through to form suitable identity or uses a method to find at least one value (e.g. cover up rule).

dM1: Full method for finding values for all three constants. Dependent on first M. Allow slips as long as the intention is clear.

A1: Correct constants or partial fractions.

(b)

M1: Splits the integral into an integrable form and integrates at least two terms to the correct form. They may use a substitution on the arctan term

A1: Fully correct Integration.

dM1: Uses the limits of 0 and 2 (or appropriate for a substitution), subtracts the correct way round and combines the ln terms from separate integrals to a single term with evidence of correct ln laws at least once.

A1: Correct answer