| Question | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: |
| 7(a) | $\|\mathbf{M}\|=2(-k-8)+1(-3-12)+1(6-3 k)=0 \Rightarrow k=\ldots$ | M1 | 1.1b |
|  | $k \neq-5$ | A1 | 2.4 |
|  |  | (2) |  |
| (b) <br> Way 1 | $\mathbf{M}=\left(\begin{array}{rrr}2 & -1 & 1 \\ 3 & -6 & 4 \\ 3 & 2 & -1\end{array}\right) \Rightarrow\left(\begin{array}{l}x \\ y \\ z\end{array}\right)=\mathbf{M}^{-1}\left(\begin{array}{l}p \\ 1 \\ 0\end{array}\right)$ | M1 | 3.1a |
|  | $\mathbf{M}^{-1}=\frac{1}{5}\left(\begin{array}{rrc}-2 & 1 & 2 \\ 15 & -5 & -5 \\ 24 & -7 & -9\end{array}\right)$ | B1 | 1.1b |
|  | $\left(\begin{array}{l}x \\ y \\ z\end{array}\right)=\frac{1}{5}\left(\begin{array}{rrr}-2 & 1 & 2 \\ 15 & -5 & -5 \\ 24 & -7 & -9\end{array}\right)\left(\begin{array}{l}p \\ 1 \\ 0\end{array}\right) \Rightarrow\left(\begin{array}{l}x \\ y \\ z\end{array}\right)=\ldots$ | M1 | 2.1 |
|  | $\left(\begin{array}{l}x \\ y \\ z\end{array}\right)=\frac{1}{5}\left(\begin{array}{l}-2 p+1 \\ 15 p-5 \\ 24 p-7\end{array}\right)$ | A1 | 1.1b |
|  | $\left(\frac{-2 p+1}{5}, 3 p-1, \frac{24 p-7}{5}\right)$ | A1ft | 2.5 |
|  |  | (5) |  |
| (b) <br> Way 2 | $\begin{aligned} 2 x-y+z=p \\ 3 x-6 y+4 z=1 \\ 3 x+2 y-z=0 \end{aligned} \quad \Rightarrow \text { e.g. } \begin{aligned} & 8 y-5 z=-1 \\ & 9 y-5 z=3 p-2 \\ & \\ & \Rightarrow x=\ldots, z=\ldots \end{aligned} \Rightarrow y=\ldots$ | M1 | 3.1a |
|  | $y=3 p-1\left(\right.$ or $x=\frac{-2 p+1}{5}$ or $\left.z=\frac{24 p-7}{5}\right)$ | B1 | 1.1b |
|  | $8(3 p-1)-5 z=-1 \Rightarrow z=\ldots \Rightarrow x=\ldots$ | M1 | 2.1 |
|  | $z=\frac{24 p-7}{5}, x=\frac{-2 p+1}{5}$ | A1 | 1.1b |
|  | $\left(\frac{-2 p+1}{5}, 3 p-1, \frac{24 p-7}{5}\right)$ | A1ft | 2.5 |


| (c)(i) | For consistency: E.g. $5 x+y=4-q$ and $15 x+3 y=q$ | M1 | 3.1a |
| :---: | :---: | :---: | :---: |
|  |  | M1 | 2.1 |
|  | $q$ | A1 | 1.1b |
|  | Alternative for (c)(i): $x=1 \Rightarrow 2-y+z=1,3+2 y-z=0 \Rightarrow y=\ldots, z=\ldots$ <br> M1 for allocating a number to one variable and solves for the other 2 $x=1, y=-4, z=-5 \Rightarrow 3+20-20=q$ <br> M1 substitutes into the second equation and solves for $q$ $\mathrm{A} 1: q=3$ |  |  |
| (ii) | Three planes that intersect in a line Or <br> Three planes that form a sheaf allow sheath! | B1 | 2.4 |
|  |  |  |  |
| 1 marks) |  |  |  |
| Notes |  |  |  |
| (a) <br> M1: Attempts determinant, equates to zero and attempts to solve for $k$ in order to establish the restriction for $k$. For the determinant, at least 2 of the 3 "elements" should be correct. <br> May see rule of Sarrus used for determinant e.g. $\|\mathbf{M}\|=(2)(k)(-1)+(4)(3)(-1)+(3)(2)(1)-(3)(k)(-1)-(2)(4)(2)-(-1)(3)(-1)=0 \Rightarrow k=\ldots$ <br> A1: Describes the correct condition for $k$ with no contradictions. Allow e.g. $k<-5, k>-5$ <br> (b)Way 1 <br> M1: A complete strategy for solving the given equations. Need to see an attempt at the inverse followed by a correct method for finding $x, y$ and $z$ <br> B1: Correct inverse matrix <br> M1: Uses their inverse and attempts the multiplication with the correct vector <br> A1: Correct values for $x, y$ and $z$ in any form <br> A1ft: Correct values given in coordinate form only. Follow through their $\boldsymbol{x}, \boldsymbol{y}$ and $z$. <br> Way 2 <br> M1: A complete strategy for solving the given equations. Need to see an attempt at eliminating one variable followed by a correct method for finding $x, y$ and $z$ <br> B1: One correct value <br> M1: Uses the equations to find values for the other 2 variables <br> A1: Correct values for $x, y$ and $z$ in any form <br> Alft: Correct values given in coordinate form only. Follow through their $\boldsymbol{x}, \boldsymbol{y}$ and $\boldsymbol{z}$. <br> (c)(i) <br> M1: Uses a correct strategy that will lead to establishing a value for $q$. E.g. eliminating one of $x, y$ or $z$ <br> M1: Solves a suitable equation to obtain a value for $q$ <br> A1: Correct value <br> (ii) <br> B1: Describes the correct geometrical configuration. <br> Must include the two ideas of planes and meeting in a line or forming a sheaf with no contradictory statements. |  |  |  |

