

Question	Scheme	Marks	AOs
9(a)	$e^{2i\theta} + e^{-2i\theta} = (\cos 2\theta + i \sin 2\theta) + (\cos(-2\theta) + i \sin(-2\theta))$ $= (\cos 2\theta + i \sin 2\theta) + (\cos 2\theta - i \sin 2\theta) = \dots$	M1	2.1
	$= 2 \cos 2\theta *$	A1*	1.1b
		(2)	
(b)	$C + iS = 1 + \frac{1}{4}e^{2i\theta} + \frac{1}{16}e^{4i\theta} + \dots$	M1	2.1
	$C + iS = \frac{1}{1 - \frac{1}{4}e^{2i\theta}}$	M1	1.1b
	$C + iS = \frac{4}{4 - e^{2i\theta}}$	A1	1.1b
		(3)	
(c)	$C + iS = \frac{4}{4 - e^{2i\theta}} \times \frac{4 - e^{-2i\theta}}{4 - e^{-2i\theta}}$	M1	2.1
	$= \frac{16 - 4e^{-2i\theta}}{17 - 4(e^{2i\theta} + e^{-2i\theta})} = \frac{16 - 4(\cos 2\theta - i \sin 2\theta)}{17 - 8 \cos 2\theta}$	M1	1.1b
	$C = \operatorname{Re} \left(\frac{16 - 4(\cos 2\theta - i \sin 2\theta)}{17 - 8 \cos 2\theta} \right) = \frac{16 - 4 \cos(2\theta)}{17 - 8 \cos(2\theta)} *$	A1*	2.2a
		(3)	
(d)	$S = \operatorname{Im} \left(\frac{16 - 4(\cos 2\theta - i \sin 2\theta)}{17 - 8 \cos 2\theta} \right) = \frac{4 \sin(2\theta)}{17 - 8 \cos(2\theta)}$	B1ft	2.2a
	$\frac{4 \sin(2\theta)}{17 - 8 \cos(2\theta)} = 0 \Rightarrow 4 \sin(2\theta) = 0 \Rightarrow \theta = \dots$	M1	3.1a
	$\theta = 0, \frac{\pi}{2}, \pi$	A1	1.1b
		(3)	

(11 marks)

Notes:

(a)
M1: Uses the modulus-argument form (Euler's formula)
A1*: Achieves the printed answer, with no errors seen

(b)
M1: Writes $C + iS$ as a series $1 + \alpha e^{2i\theta} + \beta e^{4i\theta}$
M1: Use the sum to infinity of a GP on their series
A1: Correct answer

(c)
M1: Multiplies top and bottom of the answer to (b) by $4 - e^{-2i\theta}$
M1: Replaces $e^{-2i\theta}$ with $\cos 2\theta - i \sin 2\theta$ and $e^{2i\theta} + e^{-2i\theta} = 2 \cos 2\theta$
A1*: Achieves the printed answer, with no errors seen
A1: Deduces the correct expression for S

(d)

B1ft: Deduces the correct imaginary part from their $C + iS$

M1: Sets $S = 0$ and uses trigonometry to find a value for θ

A1: All three correct values for θ