

5. The curve  $C$  has equation

$$y = \arccos\left(\frac{1}{2}x\right) \quad -2 \leq x \leq 2$$

(a) Show that  $C$  has no stationary points.

(3)

The normal to  $C$ , at the point where  $x = 1$ , crosses the  $x$ -axis at the point  $A$  and crosses the  $y$ -axis at the point  $B$ .

Given that  $O$  is the origin,

(b) show that the area of the triangle  $OAB$  is  $\frac{1}{54}(p\sqrt{3} + q\pi + r\sqrt{3}\pi^2)$  where  $p$ ,  $q$  and  $r$  are integers to be determined.

(5)