```
1 + z + z^2 + z^3 +
(b) Given that z = \frac{1}{2}(\cos\theta + i\sin\theta),
            use the answer to part (a), and de Moivre's theorem or otherwise, to prove that
                                   \frac{1}{2}\sin\theta + \frac{1}{4}\sin 2\theta + \frac{1}{8}\sin 3\theta + \dots = \frac{2\sin\theta}{5 - 4\cos\theta}
                                                                                                                                     (5)
```

(ii) show that the sum of the infinite series $1 + z + z^2 + z^3 + \dots$ cannot be purely

9. (a) Given that |z| < 1, write down the sum of the infinite series

imaginary, giving a reason for your answer.