

Question	Scheme	Marks	AOs
2(a)(i)	$a \cos^2 \frac{\pi}{3} = 1 \Rightarrow a = \dots$ or $a \cos^2 \frac{\pi}{6} = 3 \Rightarrow a = \dots$	M1	3.4
	$a = 4$	A1	2.2b
(ii)	$b \tan \frac{\pi}{3} - b \tan \frac{\pi}{6} = 2 \Rightarrow b = \dots$	M1	3.4
	$b = \sqrt{3}$	A1	2.2b
		(4)	
(b)	$V = \pi \int x^2 dy = \pi \int 16 \cos^4 \theta \times \sqrt{3} \sec^2 \theta d\theta$	M1	3.4
	$= 16\pi\sqrt{3} \int \cos^2 \theta d\theta$	A1	1.1b
	$= 16\pi\sqrt{3} \int \frac{\cos 2\theta + 1}{2} d\theta$	M1	3.1a
	$= 8\pi\sqrt{3} \left[\frac{1}{2} \sin 2\theta + \theta \right]$	A1	1.1b
	$= 8\pi\sqrt{3} \left[\frac{1}{2} \sin 2\theta + \theta \right]_{\frac{\pi}{6}}^{\frac{\pi}{3}} = 8\pi\sqrt{3} \left(\frac{\sqrt{3}}{4} + \frac{\pi}{3} - \frac{\sqrt{3}}{4} - \frac{\pi}{6} \right)$	M1	3.4
	$= \frac{4\pi^2\sqrt{3}}{3} = 22.8 \text{ cm}^3$	A1	1.1b
		(6)	

(10 marks)

Notes

(a)

M1: Interprets the information from the model and uses the parametric form of x to determine the value of a

A1: Correct value for a

M1: Interprets the information from the model and uses the parametric form of y to find b

A1: Correct value for b

(b)

M1: Uses the correct volume of revolution formula and the parametric equations for the model

A1: Correct simplified integral

M1: Uses a correct double angle identity on the integrand to achieve a suitable form for integration

A1: Correct integration

M1: Correct use of correct limits according to the model

A1: Correct volume (allow exact or awrt 22.8)